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# SOCIÉTÉ FRANÇAISE ÉTUDES ET DE RÉALISATIONS D'INVENTIONS

**COANDA** 





12, RUE LÉON BLUM, CLICHY (Seine) - FRANCE

MONITORING AGENCY DOCUMENT Nr. ASTIA DOCUMENT Nr.

## ANALYSIS OF THRUST DUE TO THE COANDA PHENCMENON Henri COANDA

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TECHNICAL REPORT
Contract Nr. AF 6I (052) - 382
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SUMMARY

The present report refers to the study of the flow in a Coanda nozzle (in different sections and along the walls) and the comparison between the effective thrust of the nozzle (directly measured on a thrust balance) and the thrust computed on the one hand from the local measurements of pressure forces on the walls, on the other hand from the velocities and pressures in terminal planes.

These tests show that the part located between the slot and the throat and called "lip" of the nozzle, is the active part of the Coanda nozzle.

#### GENERAL DESCRIPTION AND OPERATING OF THE COANDA NOZZLE

Present Contract refers to a Coanda nozzle of the 70/84 type. (See Figure No. 1).

The important element of the nozzle is the convergent section. This convergent section is composed of two distinct parts :

- the first part is the entrance,
- the second part is the fixed lip with a special profile conducting the primary flow,

between these two parts lies an adjustable slot through which the primary air arrives from an annular chamber constructed around the convergent section and constituted by the two said parts screwed on into the other. To control the slot opening it is possible to loosen or tighten the top, or first part, which is therefore called the cap.

The divergent section is a simple conic element which completes the nozzle.

Compressed air is sent into the chamber of the nozzle and emerges from the slot (primary flow). This primary flow is determined by a given slot opening and a given pressure ratio, the air in the chamber being at ambient temperature. The jet of primary air follows the profile of the lip inducing a part of the surrounding air. The resulting mixture passes through the nozzle, the flow rate measured at the exit of the divergent section being the total flow (primary air + secondary air). The mass flow thus created exerts a force on the nozzle. The component of this force in the direction of the axis of the nozzle is called the <a href="https://dx.nih.gov/html/>HRUST">HRUST</a> (F).

#### PURPOSE OF THE RESEARCH PROGRAM

The object of this survey is to analyse the thrust due to the Coanda Effect.

The tests have been performed on a Coanda nozzle of the 70/84 type with a given slot opening of 0.6 mm at two given pressures of primary air.

1. 
$$\frac{P_1 - P_0}{P_0} = 1.5$$
 (supersonic slot flow)

2. 
$$\frac{P_1 - P_0}{P_0} = 0.3$$
 (subsonic slot flow)

The measurements undertaken were as follows 8

- I. THRUST MEASUREMENTS F ON A BALANCE (exact value ± 0.030 kg.)
- 2. MEASUREMENTS OF STATIC PRESSURES ON THE WALLS The projection Fx on the axis of the resultant of all the forces due to the pressure (we consider as positive the forces constituting thrust) permits a calculation of the total axial resultant of skin friction forces (Tw) which is the difference between Fx and F, F and Fx working in the same direction and Tw constituting a drag:

Algebrically, 
$$F = Fx + Tw$$
.

The absolute experimental approximations for such measurements depend of the accuracy of the manometer reading that was about  $\pm$  0.5 mm on the mercury scale and  $\pm$  1 mm on the water scale, and during our best measurements the variation of the measured pressures was  $\pm$  1.5 mm of mercury and  $\pm$  5 mm of water, i.e., a total approximation of about :

for 
$$\frac{P_1 - P_0}{P_0}$$
 = I.5, the approximation is  $\frac{+}{}$  0.300 kg on Fx

for 
$$\frac{P_1 - P_0}{P_0} = 0.3$$
, the approximation is  $\pm 0.170$  kg on Fx

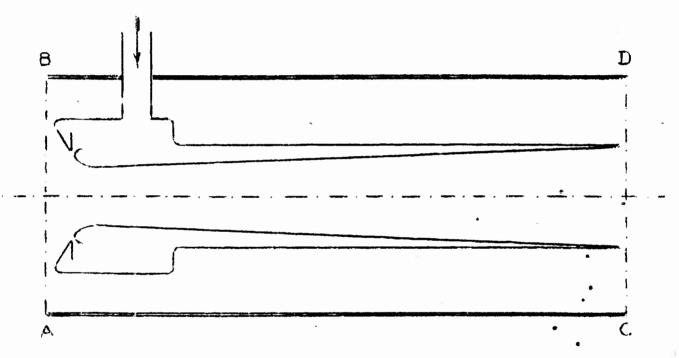
To this absolute approximation, we must add a relative approximation ± 1% due to the integration.

3. MEASUREMENTS IN PLANES 1 and VI substituted to the entrance plane and to the exit plane.

From measurements of temperatures, static and stagnation pressures, we calculate velocities.

To determine whether the Euler theorem can be applied to analyse the whole flow in such an apparatus, we chose a surface of control whose limits are a cylinder parallel to the axis of the nozzle and two planes AB and CD, perpendicular to the axis, located respectively immediately upstream of the entrance section and immediately downstream of the exit section.

(See Figure No. 2 below)



We determined in each one of these planes the term I=MV+PA momentum + forces due to the pressure in the jet.(\*) The thrust calculated corresponds to the difference between I at exit section ( $I_{CD}$ ) and I at entrance section ( $I_{AB}$ ), that is to say:

(\*) See glossary of symbols - Page B.

After the first measurements made at the entrance section and at the exit section, with the nozzle operating both in an open room and with the nozzle exit section attached to a wall, we were led, neglecting the momentum of the surrounding air, to substitute for AB the section 1 at the entrance and to substitute for AC, section VI at the exit, because the approximation of the test measurements introduced a greater error than did the influence of the momentum of the surrounding air.

4. SAME MEASUREMENTS IN THE NOZZLE - PORTIONS 1 to II, II to III and III to VI.

Due to the difficulties of measurements in the section of the nozzle right where the slot lies, we came to separate the survey of the nozzle into 3 portions according to the schematic figure (Figure No. 1) limited by the internal walls of the nozzle and the sections 1, II, III and VI, i.e. portion 1 to II, portion II to III, and portion III to VI, in order to compute separately all the conditions of the total flow :

- 1. In the convergent section just ahead of the slot or exit of primary air (Portion 1 to II)
- 2. In the second part of the convergent (total secondary air (Portion II to III)
- 3. In the divergent section (the mixture of primary and secondary air) (Portion III to VI).
- 5. THE SAME MEASUREMENTS WERE MADE IN SECTIONS IV and V, for a more complete survey of the divergent section.

Errors of approximation in measuring static pressure, stagnation pressure, thus in velocities, flow rate, momentum, pressure forces in the section: Due to the variation of the flow, it is not possible to consider a mean value of error on pressure measurements only. - Nevertheless, taking into account the error due to a possible mistake of 3° on the direction of the flow in 1 and II, the error due to the instability of pressures in III (2 to 3 mm lg), and the error due to the instability of stagnation pressure in VI, let us admit an error of 3 % on the force PA, Q and V, and therefore greater error on the momentum MV.

#### APPARATUS AND TECHNICS OF MEASUREMENTS

1. INSTALLATION FOR MEASURING THRUST - PENDULAR SYSTEM (Figure No. 3)

This apparatus is of similar principle that the one used in the tests performed under Contract No. AF 6I (052) - I58. It consists of a hollow pendular device connected with a balance capable of measuring stresses. (This hollow pendular device has been lengthened

measuring stresses. (This hollow pendular device has been lengthened so as to increase considerably the sensitivity of the whole system (1.50 m. to 2.50 m).)

The hollow pendular device itself is connected with the feed source of the pressurised fluid, which fluid passes through calibrated flowmeters, and the amount of the fluid (air) coming from the feed is controlable in quantity as well as in pressure by a system of valves. Pressure and temperature gauges complete the installation (See Figure No. 3 - General Installation).

In such a system it was absolutely necessary to be precise with the articulation D (Figure No. 4) so that it would be completely tight, to be extremely sensitive. The compressed air is fed through a lateral inlet (I) into a fixed central tube (2) rigidly fixed on two supports (3). On to this axial tube through which a hole (4) is made, a second tube (5) is placed at the center of which the hollow shaft (6) of the pendulum is attached. The first tube had on its periphery a series of annular grooves (7) which in conjunction with the interior of the second tube (5) are used as expansion chambers (8). Some of these expansion chambers are fitted with (9) floating bronze piston rings. On the right and on the left of the hole, through which the air comes to the shaft of the pendulum (6) are two lubrication points (IO).

The apparatus can constantly by brought back to zero, in order to ensure the measurements of greatest accuracy. The zero reading was obtained by the installation of tell-tale red and blue lights which are mounted directly on an arm tightened to the perpendicular re-set, so as to ensure the verticality of the vertical arm tightened to the scale by means of a magnet.

We checked the balance accuracy: the nozzle being at rost, we created an artificial thrust by means of various loads acting on the nozzle through a nylon string on a pully used as a frictionless perpendicular re-set. The whole system is constantly brought back to zero as with real thrust. The checks were made with increasing and then decreasing loads. This checking states that our thrust measurements are performed with an accuracy of ± 0.030 kg.

2. INSTALLATION FOR MEASURING STATIC PRESSURES ON THE WALL.

We determined on a first nozzle all the pressures pick ups for the survey of the skin pressures,

- all the points of measurements of the static <u>internal</u> pressures along the walls are reported on the general view Figure No. 5. Special view of these connections on the cap and on the lip are shown on Figure No. 6.
- all the points of measurements of the external skin pressures are shown on general view Figure No. 5 (four circular grooves were formed, in each of which two diametrically opposed holes were drilled, one for opening the chamber to the surrounding air, one connected to the pressures gauges).
- 3. INSTALLATION FOR MEASURING STATIC PRESSURES AND STAGNATION PRESSURES IN THE TEST SECTIONS, on a second nozzle.

Pressure probes where made by the E.N.S.A. Laboratory.

Total pressure probes of appropriate geometry permit a determination of both characteristics of the velocity: magnitude and direction.

- For the planes I and VI a special apparatus is constructed with a circular groove on which a special device is able to move the pressure probes millimeter by millimeter with great accuracy so that it is possible to know exactly the point where the measurements are made.

This special device itself can move in the circular groove around the section. (See Figures No. 7 and 7bis).

- For the survey of planes II and III, it was necessary to drill the body of the nozzle to accommodate a large pipe so as to be able to introduce the special apparatus necessary for the survey of the flow inside of the nozzle.

The hole is slightly downstream of the throat in order to introduce a tube inside of which the pressure probes and thermocouples should be introduced to study the flow at the slot and at the throat without disturbing the flow.

Outside of the nozzle the same special device is mounted to move millimeter by millimeter the pressure probes and thermocouples (See Figure No. 7).

- For the planes IV and V, the installation for measurements is the same. (See Figure No. 7).

#### 4, INSTALLATION FOR MEASURING TEMPERATURES.

The thermocouples are Constantan and Lianganin wires (I/IO mm). Measurements are recorded by apparatus Kipp Micrograph D.D.3.

As noted above for pressure measurements, a special device was used capable of moving thermocouples millimeter by millimeter with great accuracy (See Figure No. 7)

In plane II other total and static pressure probes and thermocouples were fitted so as to study the jet flow near the wall in proximity of the slot section, but due to the discontinuity of the jet flow in that section all pressures measurements were so much disturbed by the presence of the probes that the resultant measurements must be considered invalid.

However, for the temperature measurements, it was possible to introduce the thermocouples by the entrance, and due to the very small size of the apparatus a good measurement of temperatures was possible.

In plane VI the flow rate of the flow was irregularly distributed and we have surveyed several diameters to obtain the mean value of these measurements.

#### RESULTS OF THE INVESTIGATION OF THE FLOW IN VARIOUS PLANES

It is to be noted that all tests were performed at the same slot opening b = 0.60 mm with two feeding pressures Pi, such that:

P1 - Po ( 0.3 corresponding to primary flow rate Q1 = 93 1/sec.

at ambient conditions (To = Po)

#### I. TEMPERATURES MEASUREMENTS.

At first we began by the temperature measurements as we had to know these values for all pressure measurements. Moreover the temperature measurements are the only ones available in plane II where the slot lies. Due to the construction we measured essentially stagnation temperature through internal sections except for the slot where we could operate in good conditions by introducing thermocouples by the entrance.

In plane II of the slot, the curve Figure No. 8 points out the masses of air of primary and secondary flow. It is obvious that near the wall, the presence of the wall itself leads us to an important error on the temperature measurements in the jet flow.

In plane III (throat), the temperature measurements are measurements of stagnation temperature (Figure No. 9).

From the pressure measurements, we determined the corresponding static temperature (Figure No. 10).

On the whole, these measurements show that the variations of temperature in planes 1 (entrance), II (convergent section), IV and V (divergent sections), VI (exit), may be neglected, because the errors noticed are lower than the difference between the temperature in the feeding chamber and the surrounding temperature ( mean value =  $0.5^{\circ}$ C).

#### 2. MEASUREMENTS OF STATIC and STAGNATION PRESSURES IN THE FLOW

Preliminary tests with and without a wall at the exit section had shown that it was not necessary to perform these measurements with a wall attached at the exit section. The curves showing the variations of the effective static pressure plotted versus the radii are reported on figure No. 11 (section 1) to figure No. 16 (section VI).

(Concerning the possible errors on these values, see page: 10.4 & 6).

#### 3. VELOCITY CALCULATION

The general aspect of the flow in the nozzle is shown Figure No. 17.

The velocities V have been calculated from the pressure measurements (static and stagnation) and from temperature measurements. - For low velocities ( Mach number  $\,\mathrm{M}\, \leqslant \, 0.3\,$ ) a simplified Bernoulli formula was used :

$$\frac{\Delta}{q}$$
  $\frac{V^2}{2}$  = Pt - Ps

For higher velocities ( Mach number M > 0.3 ) the Saint-Venant formula was used :

$$\frac{Pt}{Ps} = \left[1 + \frac{\chi - 1}{2} M^2\right] \frac{\chi}{\chi - 1}$$

The Saint-Venant formula was used in Planes III and IV.

The curves showing the velocities plotted versus the radii are reported on Figure No. 18 (section 1) to Figure No. 23 (section VI)

Figure No. 23bis shows the variation of velocities on a diameter of section VI, the nozzle operating in an open room, and the nozzle having the exit section attached to a wall.

The curves (Figures No. 18 to 23) showing the variation of velocities and the curves (Figures No. 11 to No. 16) showing the variation of static pressure have approximately the same general aspect. In sections 1 and II where stagnation pressure is constant and equal to the atmospheric pressure, velocities are reciprocal to the square root of static pressures.— However, in section VI where the variations of static pressure are very small and about zero (always 2g./cm²) the velocity varies with the square root of stagnation pressure, which explains the different aspect of Figures No. 16 and No. 23.

#### 4. FLOW RATE CALCULATION.

Before other calculations we consider as essential to confirm the validity of our measurements by applying the fundamental continuity formula. If we assume that the primary flow rate Q1 is perfectly known (absolute value of error  $\[ \] \frac{1}{2} \] \]$ , Q1 being the primary flow rate corrected at the surrounding conditions Po To, and if we measure the flow rates in the various sections (corrected at the surrounding conditions: D1 in section 1, D11 in section II, D111 in section III, D121 in section VI), the continuity formula is to be written:

$$D_1 = D_{II} = D_{III} - Q_1 = D_{IV} - Q_1 = D_V - Q_2 = D_{VI} - Q_1$$

To calculate these flow rates we were led to draw the curves V plotted versus R<sup>2</sup>, whence we compute by graphic summing up the flow rate as

where  $\Delta$  and  $\Delta_a$  are the specific weights respectively at local conditions and at surrounding conditions. See curves Figure No.24 for section 1 to figure No.29 for section VI.

The following table gives the results of the computation of the mean value of the total flow rate in 1/sec. at surrounding conditions (Po To).

We were able to determine the induction ratio  $Q_2$  which is the ratio of  $Q_2$  to  $Q_1$ , i.e.,  $Q_1 = \frac{Q_2}{Q_1}$ 

P1-Po Po	Q1 1/s	D <sub>1</sub> 1/s	DII 1/s	D <sub>III</sub> -Qı 1/s	D <sub>TV</sub> -Q1*	Dv-Q1** 1/s	Dyr-Qı 1/s	Q <sub>2</sub> 1/s	٩
1.5	93	616	606	599	631	607	635	617	7.6
0.3	38	297	287	291	308	282	303	292	8.7
1		l .							

- In these two planes, which are in the divergent section, the error can be greater and can reach 4 % as the flow begins to be less regular and it was only possible to take measurements on one diameter.
  - In planes III and VI, the errors are of the same magnitude as in plane 1 and II, i.e. about 3 %.

#### 5. CALCULATION OF MOMENTUM MV AND OF PRESSURES FORCES PA

gives for MV, PA, I, the following table :

We have computed in each section the terms MV and PA with a view to compare the variation of the term I with the resultant of the forces due to the pressure exerted on the walls between two sections (See page No. 6)

These curves are represented on Figures No. 30 to 4I, in which the values corresponding to the variation of Ps - Po plotted versus the square of the radii are respectively plotted on the drawings Figures No. 30 to 35 for the sections 1 to VI, and the variation of the term Av plotted versus the square of the radii are on the drawings Figures No. 36 to No. 4I for the section 1 to VI which

	<u>P1 - P0</u> P0	MV	РА	I
1	I,5	+ 2.750 kg	- 2.180 kg	+ 0.570 kg
II	I.5	+ 4.750 kg	- 3.290 kg	+ I.460 kg
III	I.5	+ 16.930 kg	- 6.570 kg	+ 10.360 kg
IV	I.5	+ II.850 kg	- 3.175 kg	+ 8.675 kg *
V	I.5	+ 7.985 kg	- I.720 kg	+ 6.265 kg *
VI	I.5	+ 6.460 kg	- 0.170 kg	+ 6.290 kg
	===i=====			
1	0.3	+ 0.620 kg	- 0.530 kg	+ 0.090 kg
II	0,3	+ I.053 kg	- 0.775 kg	+ 0.280 kg
III	0.3	+ 4.130 kg	- I.I55 kg	+ 2.975 kg
IV	0,3	+ 2.500 kg	- 0.710 kg	+ I.790 kg *
V	0.3	+ I.670 kg	- 0.420 kg	+ I.250 kg *
VI	0•3	+ 1.580 kg	- 0.060 kg	+ 1.520 kg

<sup>\*</sup> for sections IV and V see notice Page No. 12.

Bearing in mind the calculated error in each plane these results are valid with approximation of 3 % on PA and 6 % or MV in the sections 1, II, III, VI, and 4 % on PA and 8 % on MV in the sections IV and V.

#### RESULTS AND THEIR DISCUSSIONS

#### I. THRUST MEASUREMENTS ON THE BALANCE

The results of these measurements are made with an approximation of  $\pm$  0.03 kg.

	b = 0	.60 mm		
<u>P1 - Po</u> Po	Qı read 1/s	Q <sub>1</sub> corrected	Tr	# a #
I.5	I28.5	92.9	5,520	1.32
I.	II2.5	72,3	4.000	I.38
0 <b>.7</b> 5 0 <b>.</b> 5	98 87	59.I 48.5	3.140 2.200	I.46 I.45
0.3	72.5	37.7	I.400	I.46
0.1	47	22,4	0,540	1.57

We chose, for the other measurements, only two feeding pressures:

$$\frac{P_1 - P_0}{P_0} = I.5 \text{ and } 0.3$$

2. INTERNAL AND EXTERNAL SKIN PRESSURES on the walls and evaluation of the axial resultant forces Fx of these pressure forces.

400

Preliminary tests had shown that the surrounding flow was not measurable.

Figure No. 42 shows a general view of the distribution of the pressures along the internal profile of the nozzle.

Figure No. 43 is a detailed view showing how pressures are distributed along the lip profile.

On Figures No. 44, 45 and 45bis, 46 and 46bis, effective pressures Pw - Po are plotted versus the square of the distance from the walls to the axis, the elementary forces will be positive if exerted in the direction of the thrust. The area included between the horizontal axis and the curves is reciprocal to the resultant Fx, elementary forces due to the pressures exerted: on the cap Figure No. 44, on the lip Figures No. 45 and 45bis, on the divergent section Figures No. 46 and 46bis.

The results are:

Curves	<u>P1 - Po</u> Po	Portion	. Resultant Fx
IO IO bis	1.5 }	cap	( + I.3I0 kg ( + 0.380 kg
ll	I <sub>0</sub> 5 )	lip	( + 8.6 kg
II bis	0.3 )		( + I.970 kg
I2	I.5 )	divergent	( - 3.170 kg
I2 bis	0.3 )		( - 0.660 kg

Taking into account the possible errors on these measurements (See page No. 4) we compare the total results Fx with thrust F measured on the balance, calculating  $T_W = F_X - F$ .

<u>P1 - Po</u> Po	F in kg	Fx in kg	Tw in kg
I.5	5.520 ± 0.030	6.740 ± 0.300	1.220 ± 0.330
0.3	1.400 ± 0.030	1.690 ± 0.170	0.290 ± 0.200

3. ANALYSIS OF THE THRUST in the whole nozzle in terms of variation of I (momentum + pressure forces)

From the value of I=MV+PA given Page No. I3 we calculate the variation  $\triangle I$  between the entrance section 1 and the exit section VI which gives the following values which we compare with the values of thrust measured on the balance.

In this portion we have :

<u>P1-P0</u> Po	ΔI = variation	F		erence - F	Fx	Tw =	F - Fx
70	of I kg between 1 and VI	kg	in kg	in terms of F	and the annex of	in kg	in terms of Fx
I.5 0.3	+ 5.720 + I.430	5.520 I.400	0.200	4 % 2 %	6.740 I.690	- I.220 - 0.290	20 % I7 %
					,		

4. ANALYSIS OF THE THRUST IN THE THREE BASIC PORTIONS 1 II, II III, III VI, in terms of variations of I ( / I ) between two successive sections which give the following value which may be compared with the values of thrust measured on the balance.

Portions			betwe minal	planes of	Fa	k kg
Portion	1	VI	+	5.720	+	6.740
Portion	1	II	+	0.890	+	0.870
Portion	II	III	+	8,900	+	9.040
Portion	III	VI	-	4.070	-	3.170
Portion	1	VI	+	I <sub>0</sub> 430	+	I.690
Portion	1	II	+	0.190	+	0.260
Portion	II	III	+	2.695	+	2.090
Portion	III	VI	-	I.455	<b></b>	0.660
	Portion Portion Portion Portion Portion Portion Portion Portion	Portion 1 Portion 1 Portion II Portion III Portion 1 Portion 1	Portion 1 VI Portion 1 II Portion II III Portion III VI  Portion 1 VI Portion 1 II Portion I III Portion II III	Portions minal the p  { Portion 1 VI +  Portion 1 II +  Portion II III +  Portion III VI +  Portion 1 II +  Portion 1 II +  Portion 1 II +	Portion   VI	Portions   minal planes of the portion   kg

Considering that  $\Delta$  I is a fair approximation of F, the difference Fx =  $\Delta$  I shows that losses due to friction are found essentially in the divergent section.

CONCLUDING REMARKS

From all the research program carried out in the present contract we can conclude that, in fact we have made a complete investigation on the air flow through a Coanda nozzle; this study points out the two following characteristics: the induction ratio and the thrust augmentation ratio.

- I. Regarding the measurements, it is necessary to notice that all the measurements (no matter what sort of measurements) have a remarkable concordance. However, the work in itself on the Coanda nozzle choosen was not at all easy. Indeed the tests as required by the contract, were performed on a Coanda nozzle 70/84 of an improved type and this for the thrust purpose but with a throat of cross section of small size (diameter \$\phi\$ 70 mm). In spite of this small dimension, the tests have been performed with a great accuracy due to the sensitivity of all the instruments, more peculiarly of the specially improved balance, and to the great carefulness brought for the measurements and the general observations.
- 2. If we consider the very encouraging results obtained, it appears that it would be quite important to ascertain the real theory of such nozzles. But, this will need an important study, which would require a special team well trained in aerodynamic and this during a fairly long time. The research would have to be done on nozzles of various dimensions having a perfect geometrical similitude.

3. It had been also observed that the flow at the exit is still distorted, as the primary and the secondary flow seem not to be completely mixed. Consequently it did appeared to us that it could be necessary to improve the mixing, wether by acting on the divergent section length or by adding a new mass of surrounding air. We have therefore fixed at the exit section a single bell (with divergent angle of 2°) and we then obtained the following thrust augmentation ratio.

NOZ.ZLE 70/84 TYPE
+ a single bell removed at I50 mm. downstream
the exit section.

	b =	0.60 mm		
<u>P1 - Po</u> Po	Q1 read Q1 1/s corrected		Tr	* 2 *
I.5	122.5	88,56	6,220	I.55
I	I05	67.5	4.460	I.64
0.75	94	56.7	3.500	I.69
0,5	83.5	46.5	2.400	I.65
0,3	70	36.4	I.560	I.68 ·
0.1	46	21.9	0.580	I.72

This puts in evidence that the contact surfaces, between primary and secondary air flow, are not in accordance and that is, probably, due to the small size of the throat section in regard of the lip surface for a given volume of primary air flow.

4. It appears also from our very careful investigations specially on the skin pressure measurements, that the lip is the part of the nozzle producing the maximum of the thrust, and that the divergent section is producing a drag working in the opposite direction.

We have also observed that the divergent section is producing nearly the totality of the losses due to the skin friction.

All this bring us to consider that it seems of great importance to increase the diameter for a given length of the divergent section.

In any case the above considerations show clearly the necessity for more systematic investigations.

This studies has been performed by the SFERI-COANDA team.

#### ACKNOWLEDGEMENT

This research program and the preparation of the Report were carried out with very valuable supervision of Professor E.A. BRUN, de la Faculté des Sciences de Paris, and using facilities made available by Mr. LEBRUN, Chef du Laboratoire d'Aérodynamique de E.N.S.A., who supervised the tests which were conducted in that Laboratory.

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#### GLOSSARY OF SYMBOLS

- $a Thrust coefficient = \frac{F}{Fo}$
- b Slot opening
- General term for air flow rate, corrected for Po, To subscript 1 to VI = flow rate through said plane

$$D_{\text{A=0}} \int_{A=0}^{A=\text{Tr} Rm} \frac{\Delta}{\Delta} V dA = \text{Tr} \int_{R=0}^{R=Rm} \frac{V \Delta}{\Delta_0} 2R dR$$

- Surface differential element for a surface limited by R and R + dR dA = 2 77 R dR
- dm mass differential element for a cylindrical ring, limited by R and R + dR, length V dm =  $2\pi \frac{\Delta}{g}$  V R dR
- dR Radius element
- F Thrust developed by the nozzle and directly measured
- Fo Theoretical thrust obtained with simple isentropic nozzle

$$F_o = \frac{\Delta}{9} Q_1 U_0 \sqrt{\frac{2}{\gamma-1} \left[1 - \left(\frac{P_1}{P_0}\right)^{-\frac{\gamma-1}{\gamma}}\right]}$$

- Fx Resultant on the axis of the forces due to the pressures on the walls
- g acceleration due to the gravity = 9.81 m/sec<sup>2</sup>
- h distance from the wall to the axis. h = Rm

	I	MV + PA
ì	M	Mach number
J	MV	Mach number  General term for momentum $MV = \int_{R_{-Q}}^{R_{-R}} \frac{\Delta}{9} V^{2} \pi R dR$
	PA	General term for
		$\int_{0}^{\infty} \frac{1}{15} \int_{0}^{\infty} \frac$
	P	General term for pressure
1	Po	Atmospheric pressure
;	P1	Pressure of feeding (primary) air
	Ps	Static pressure in the jet
	Pt	Stagnation pressure in the jet
	Pw	Pressure along the skin
•	Q1	Primary air flow rate, corrected for Po, To
(	$Q_2$	Total air flow rate, corrected for Po, To
!	R	Radius
1	Rm	Maximum value of R in a section, Rm = h
	Tw	Skin friction losses
	т	General term for temperature

Stagnation temperature

To Ambient temperature

Ts

Tt

Static temperature

Tch Temperature in chamber, generally equal to To

U Local sound velocity

Uo Sound velocity at ambient temperature To

V Velocity

Δ Local specific weight of air

 $\Delta_{f e}$  Specific weight of air for Po, To

ΔΙ Variation of I, between two sections

Ratio of specific heats, here % = I.4

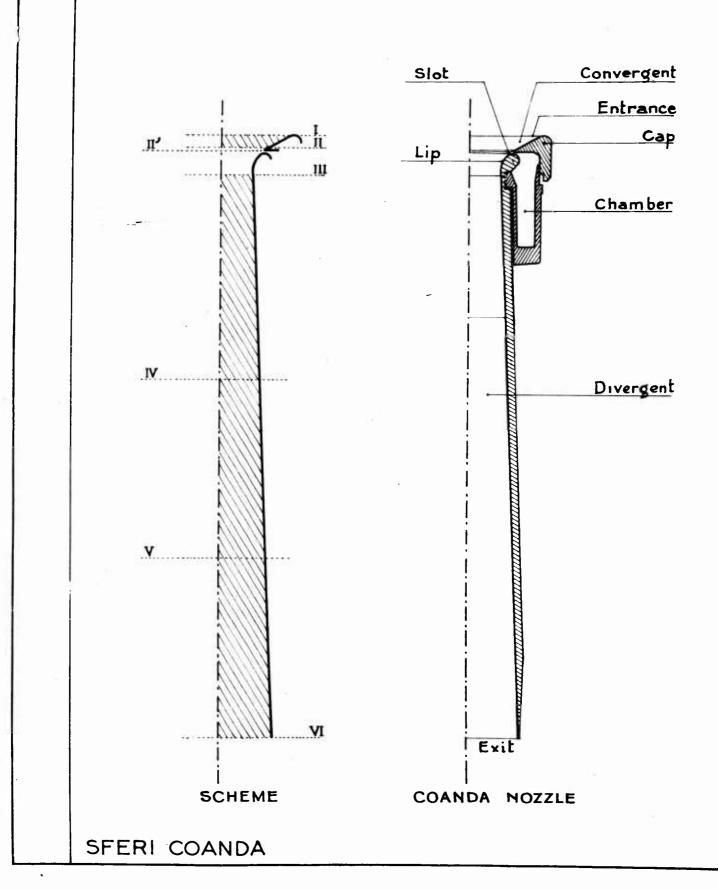
P Induction ratio =  $\frac{Q_2}{Q_1}$ 

#### LIST OF ILLUSTRATIONS

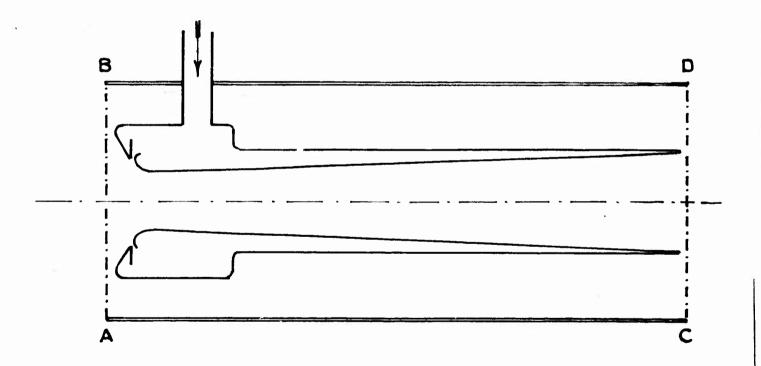
No. of Figures	Title
1	General description of a Coanda nozzle
2	Schematic of the entrance and exit planes of survey
3	Pendular system for measuring thrust
3bis	Photograph of pendular system
4	Detail of 3 - Articulation D
5	View of the points of measurements of the static internal and external skin pressures
6	Detail of 5 - Points of measurement on the lip
7	Special device for introducing the measurement instruments
7bis } 7ter }	Photographs of 7 mounted on the nozzle - General view
8	Static temperatures (Ts - Tch) in section II' (slot) plotted versus radii R
9	Stagnation temperatures (Tt - Tch) in section III (throat) plotted versus radii R
ю	Static temperatures (Ts - Tch) in section III (threat) plotted versus radii R
11 to 16	Effective pressure (Ps - Po) plotted versus radii R
II	Section 1
12	Section II
13	Section III
14	Section IV
15	Section V
16	Section VI

No. of Figures	Title (continued)
17	General aspect of the flow
I8 to 23	Velocities V plotted versus radii R
18	Section 1 (velocities projected on the axis)
I8bis	Section 1 (velocities and their projection)
19	Section II (velocities projected on the axis)
20	Section III
21	Section IV
22	Section V
23	Section VI - mean value
23bis	Section VI on a diameter with and without a wall attached at the exit section
24 to 29	Computation of the corrected flow rate:  V
24	Section 1 $\Delta_o$
25	Section II
26	Section III
2 <b>7</b>	Section IV
28	Section V
29	Section VI
30 to 35	Calculation of PA; (Ps - Po) plotted versus R2
30	Section 1
31	Section II
32	Section III
33	Section IV
34	Section V
35	Section VI

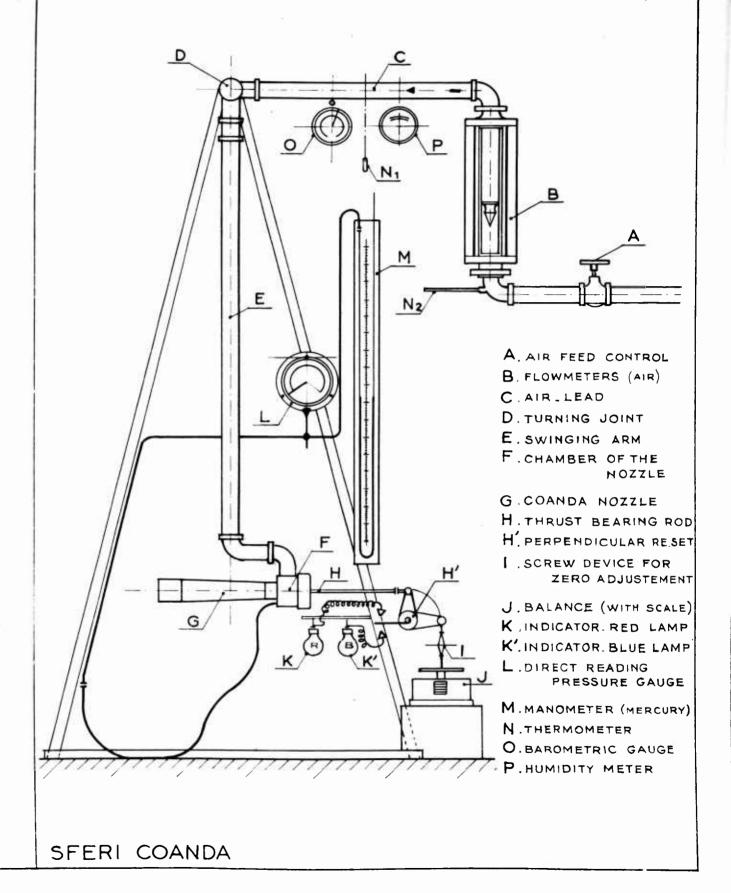
Nc. of Figures	Title (continued)
36 to 4Ibis	Calculation of MV: V <sup>2</sup> plotted versus R <sup>2</sup>
36	Section 1 A.
3 <b>7</b>	Section II
38	Section III
39	Section IV
40	Section V
41	Section VI
42	General view of the distribution of the pressure along the internal profile of the nozzle
43	Detail of Figure No. 42, along the lip profile
44 to 46bis	Effective pressures (Pw - Po) plotted versus the square of the distance from the wall to the axis
44	on the cap $\frac{P_1 - P_0}{P_0}$ = I.5 and 0.3
45 45bis	on the lip $\frac{P_2 - P_0}{P_0} = \begin{cases} I_05 \\ O_03 \end{cases}$
46 46 <b>bi</b> s	on the divergent $\frac{P_1 - P_0}{P_0}$ at $\begin{cases} I.5 \\ 0.3 \end{cases}$

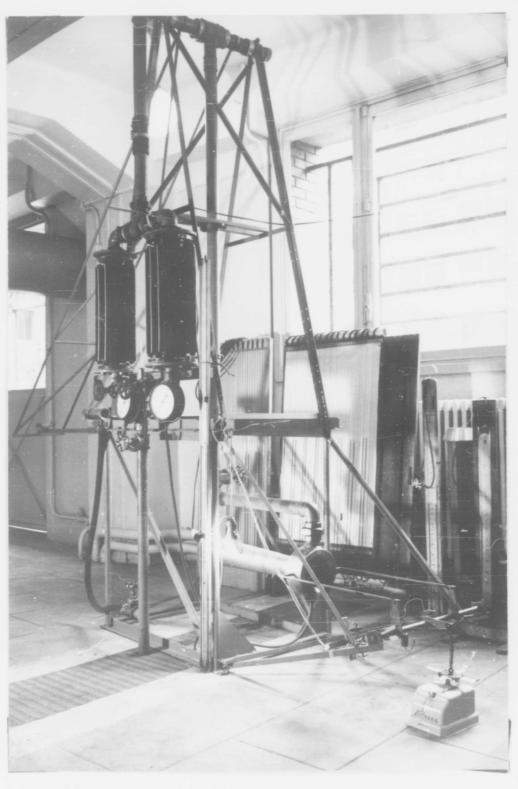


SCHEMATIC OF THE TERMINALS PLANES OF THE SURVEY.

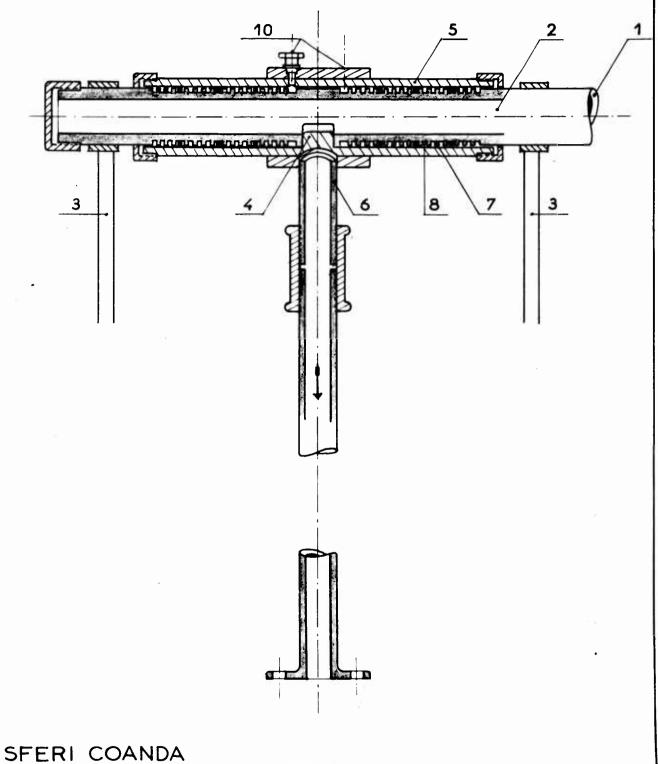


SFERI-COANDA.

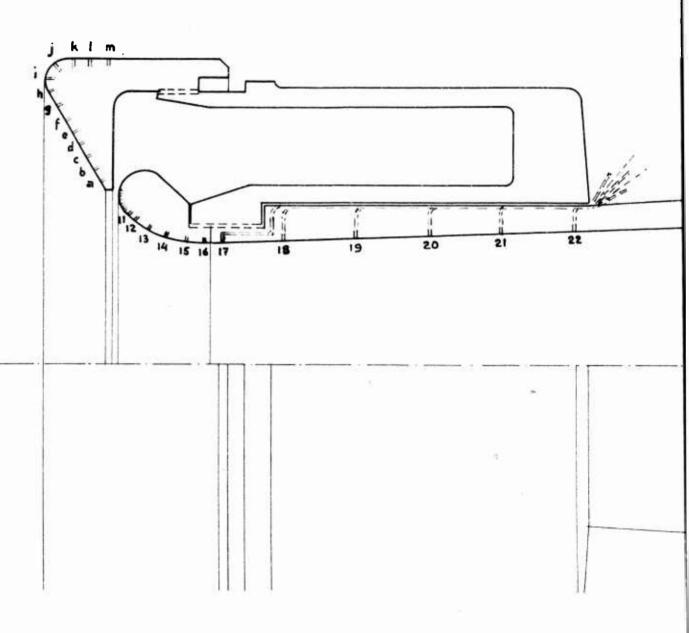




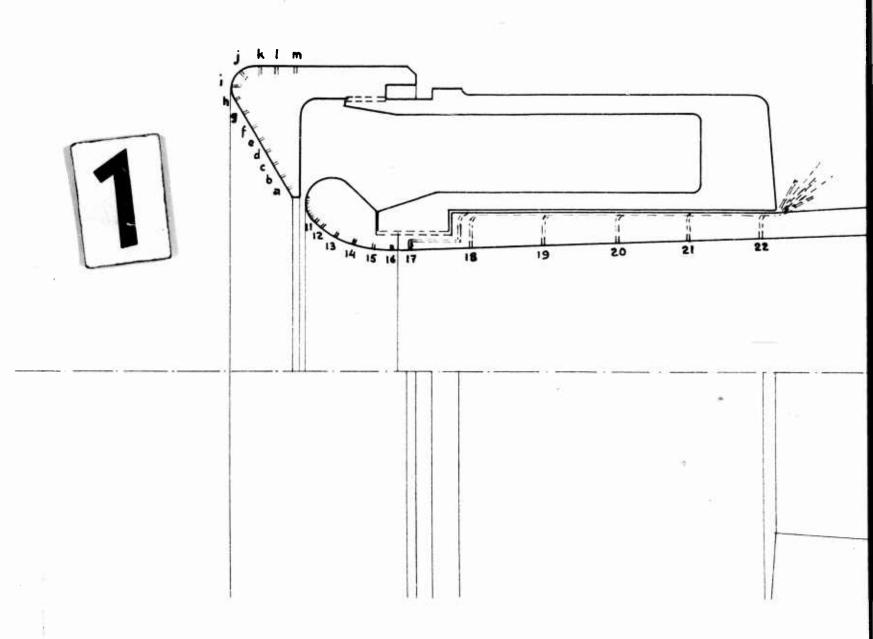
THE TURNING JOINT D

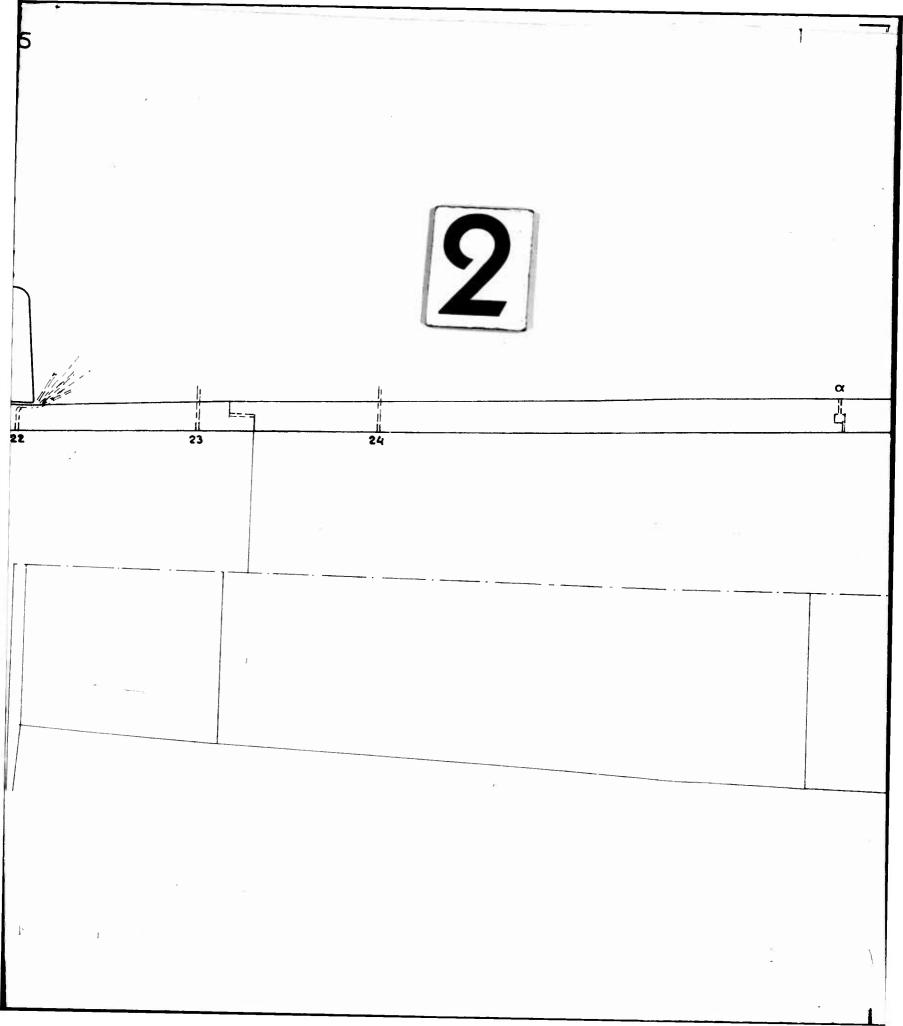


View of the points of measurements of the static skin pressures on the internal and external walls.

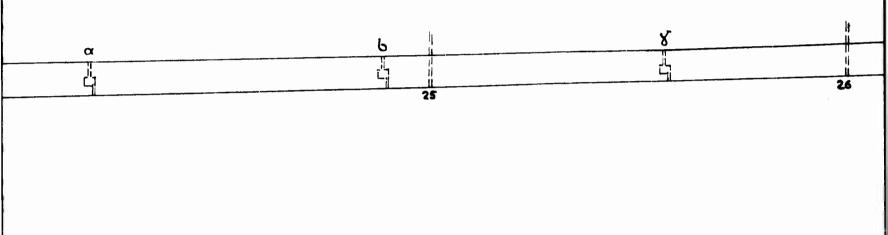


View of the points of measurements of the static skin pressures on the internal and external walls.

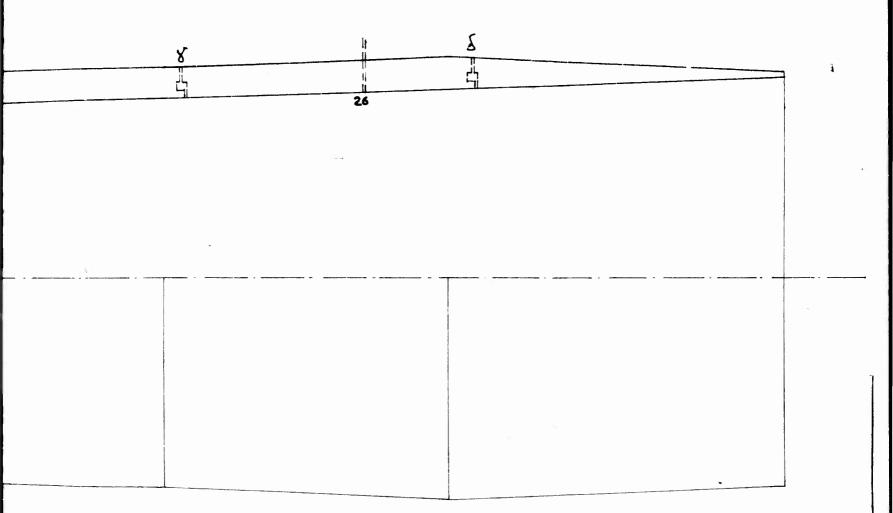


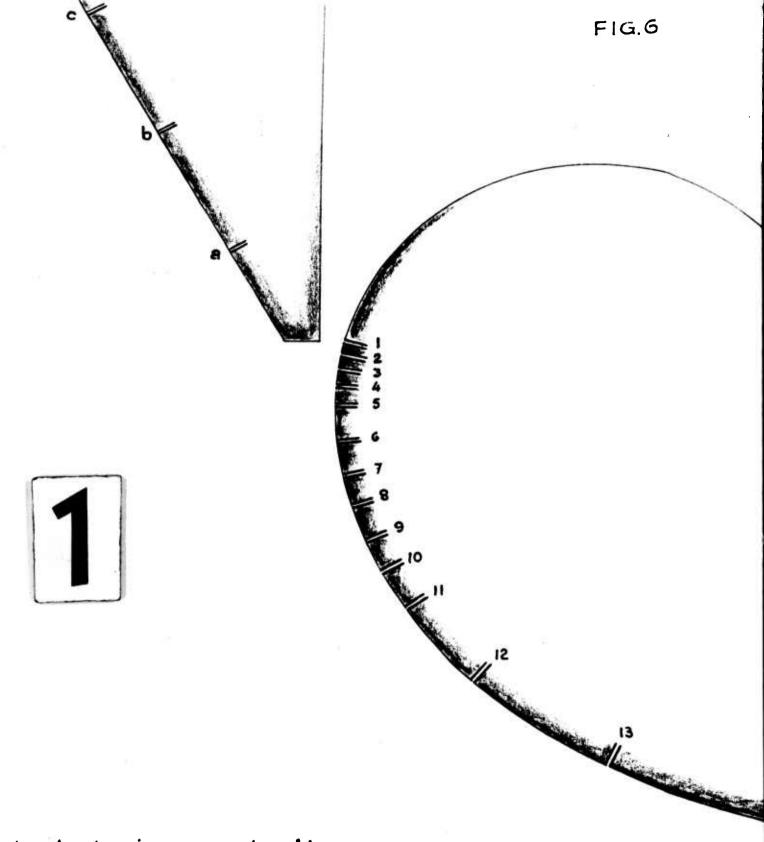












Detailed view of the lip.

SFERI COANDA.



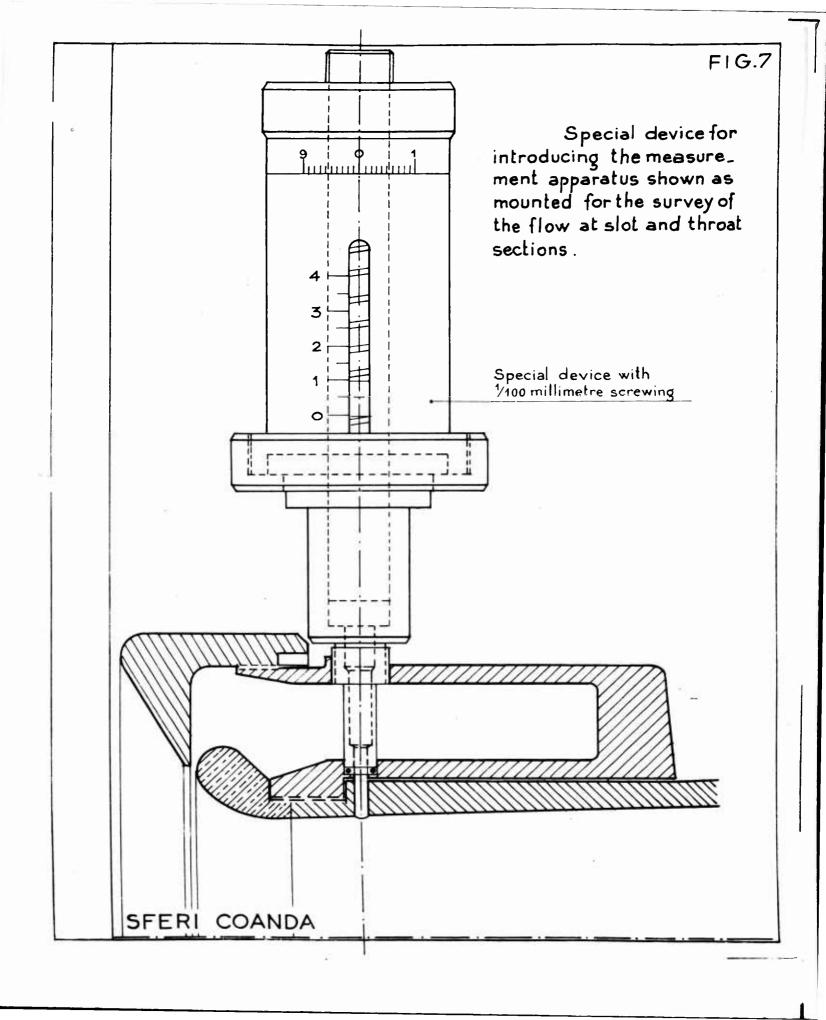
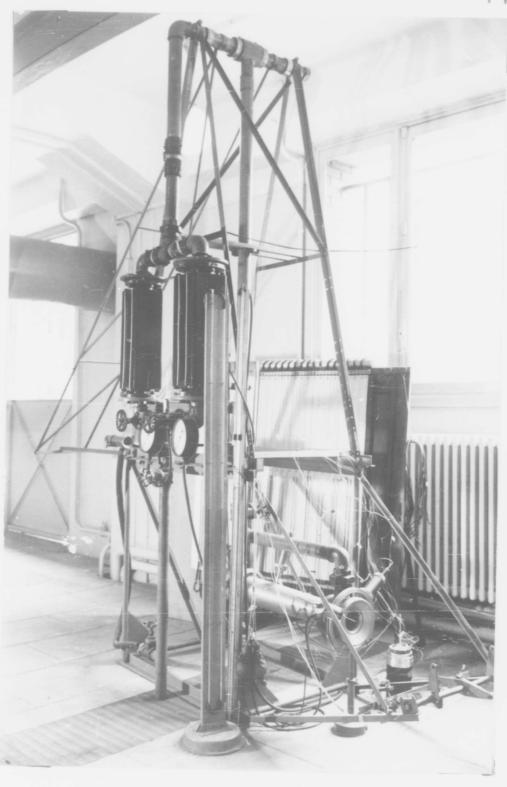
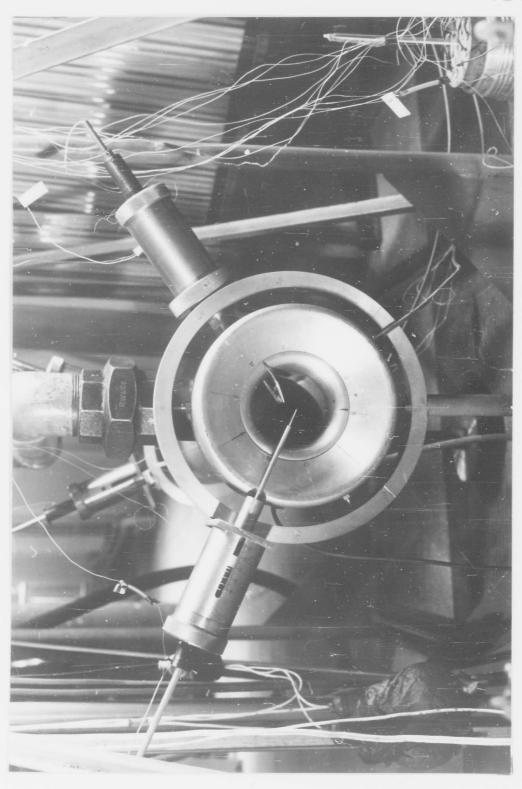


FIG 7 bis



SFERI-COANDA



SFERI-COANDA.

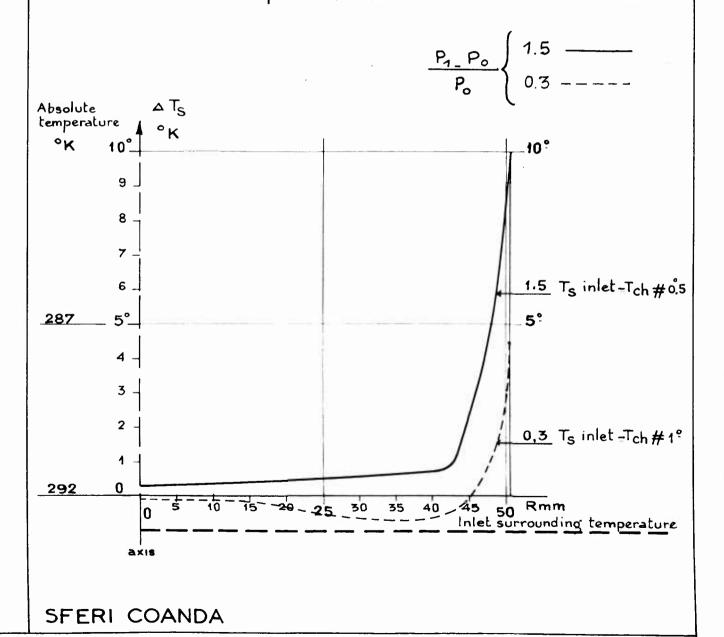
# SLOT SECTION (II')

Approach of the temperature

Variation of relative static temperature

plotted versus the radii

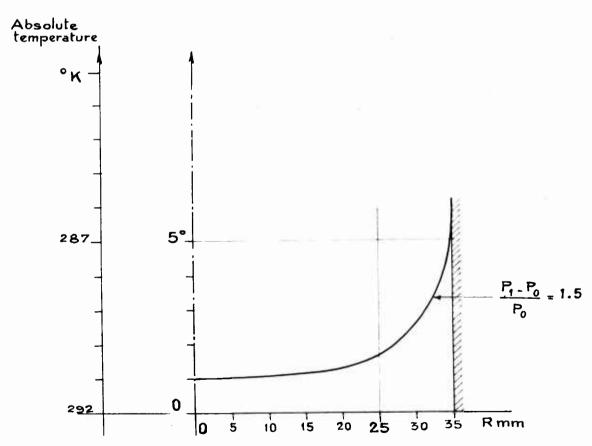
 $\Delta T_s$  °K versus Rmm  $\Delta T_s = T_s$  at the point of measurement \_T in the chamber



# THROAT SECTION (III)

Variations of total temperatures plotted versus the radii

 $\Delta T_t$  oK versus Rmm  $\Delta T_t = T_t$  at the point of measurement \_T in the chamber

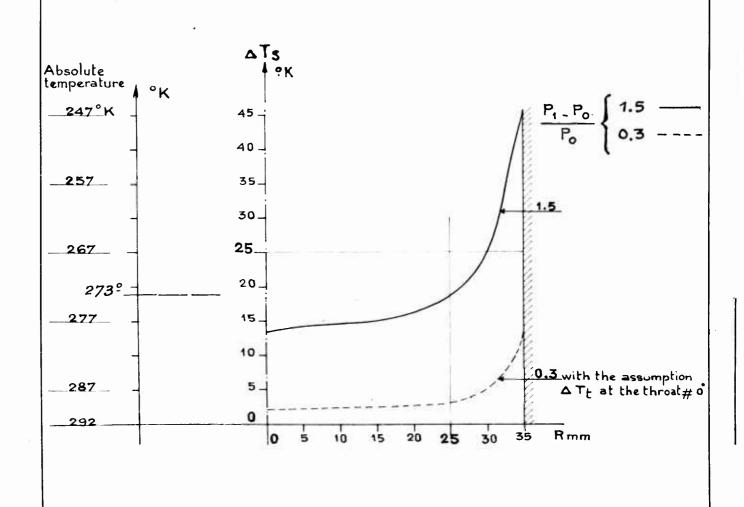


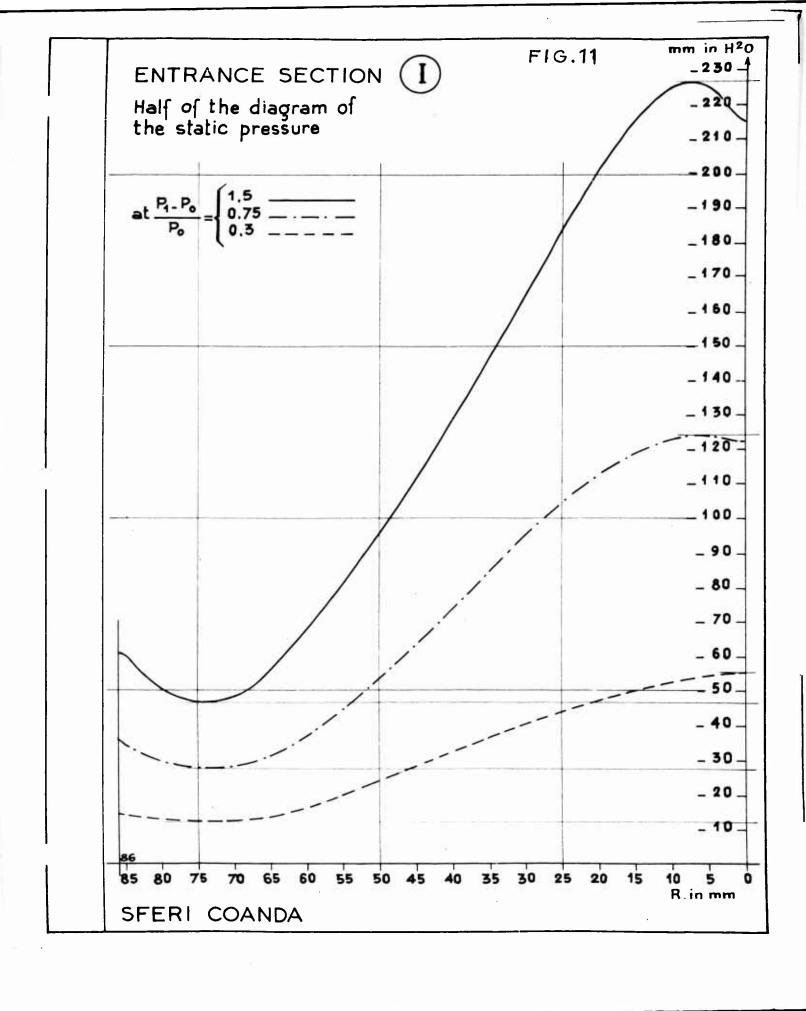
No valable measurement at  $\frac{P_1 - P_0}{P_0} = 0.3$  due to the low value of  $\Delta T_t$ 

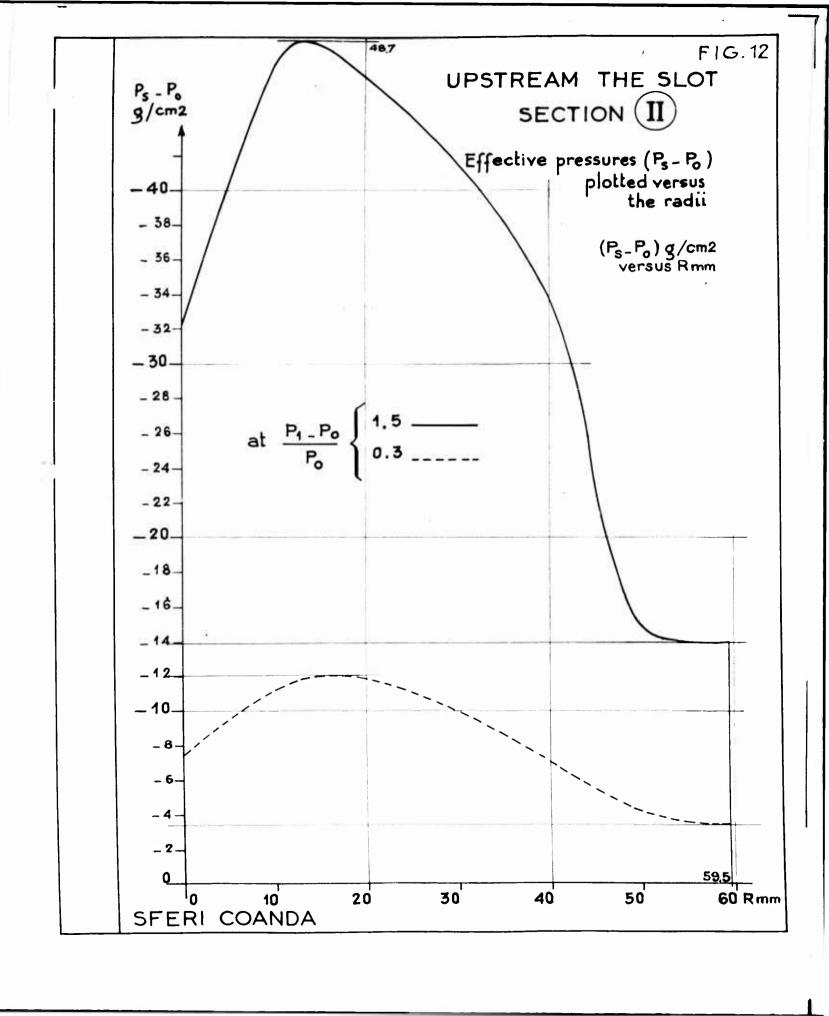
Approach of the temperature

Computed values of static temperatures

plotted versus the radii

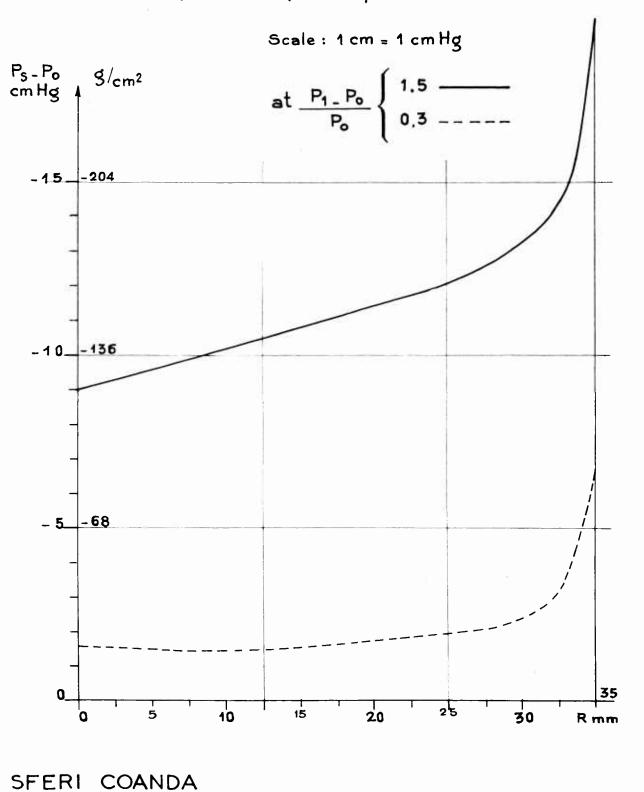








Effective pressures (Ps-Po) plotted versus the radii



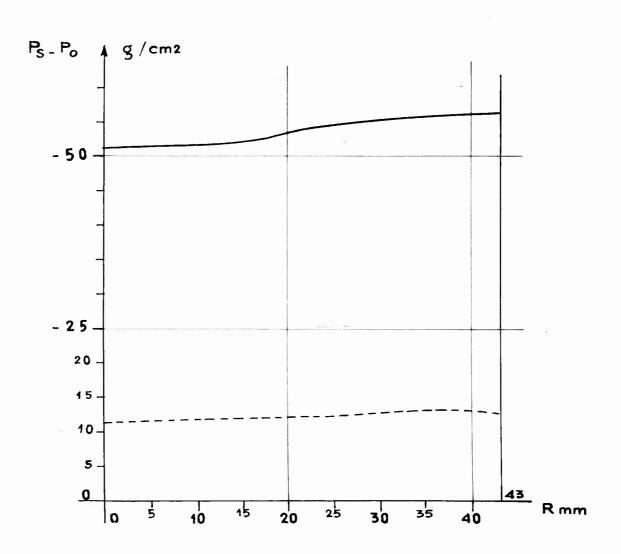
#### UPSTREAM SECTION IN THE DIVERGENT



Effectives static pressures plotted versus radii

P<sub>s-P<sub>o</sub></sub> g/cm<sup>2</sup> versus Rmm Scale: 1cm = -5g/cm<sup>2</sup>

at 
$$\frac{P_1 - P_0}{P_0} \begin{cases} ---- 0.3 \end{cases}$$



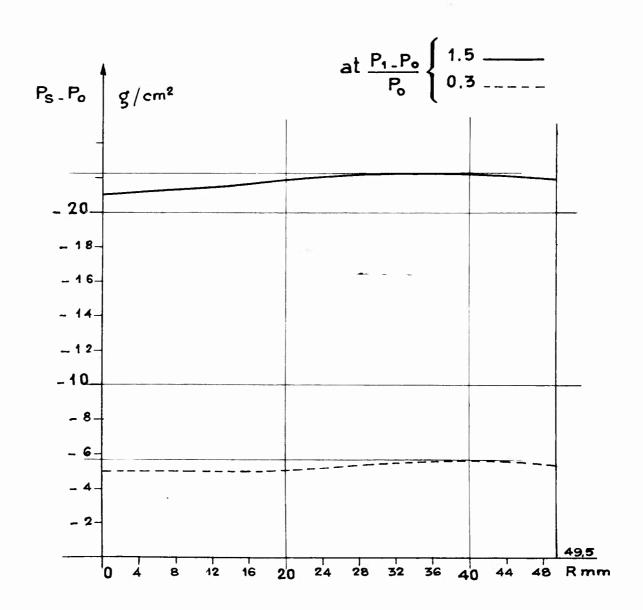
#### DOWNSTREAM SECTION OF THE DIVERGENT



Effective static pressures plotted versus radii

Ps-Po g/cm² versus R mm

Scale : 1 cm = 2g/cm2

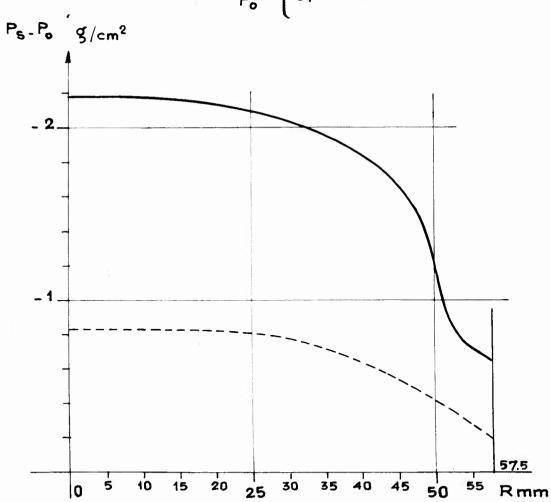


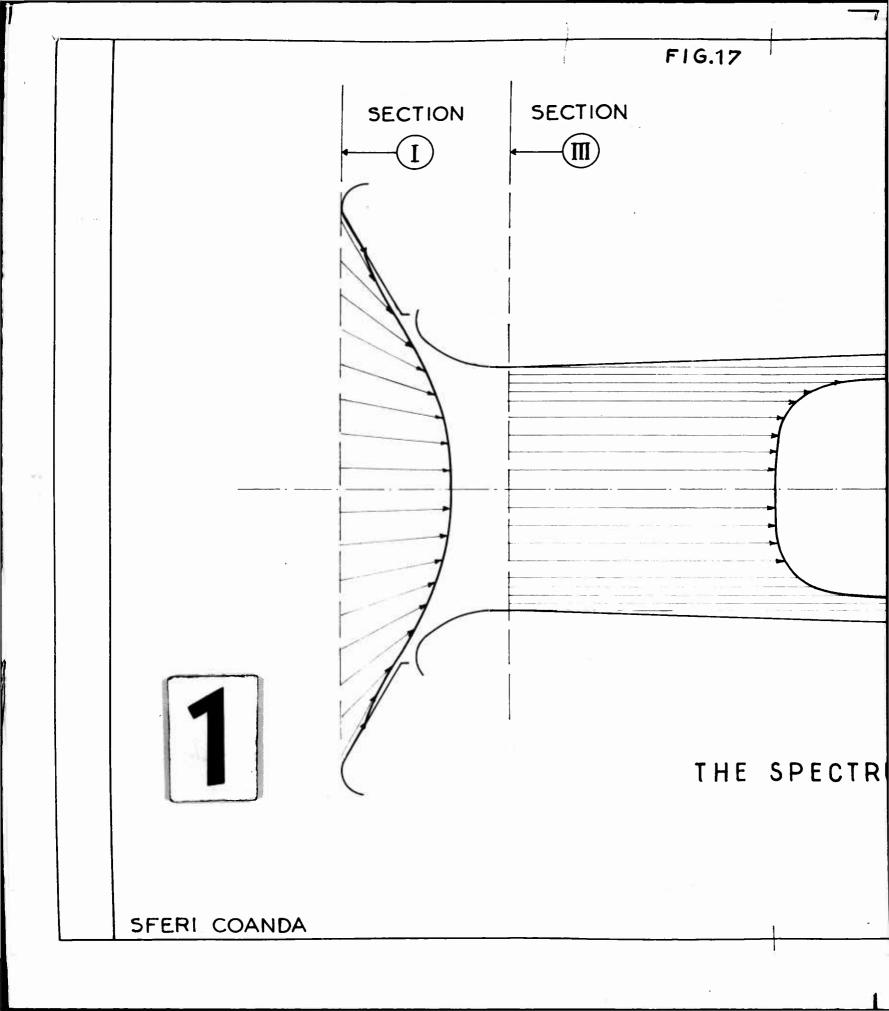
# EXIT SECTION (VI)

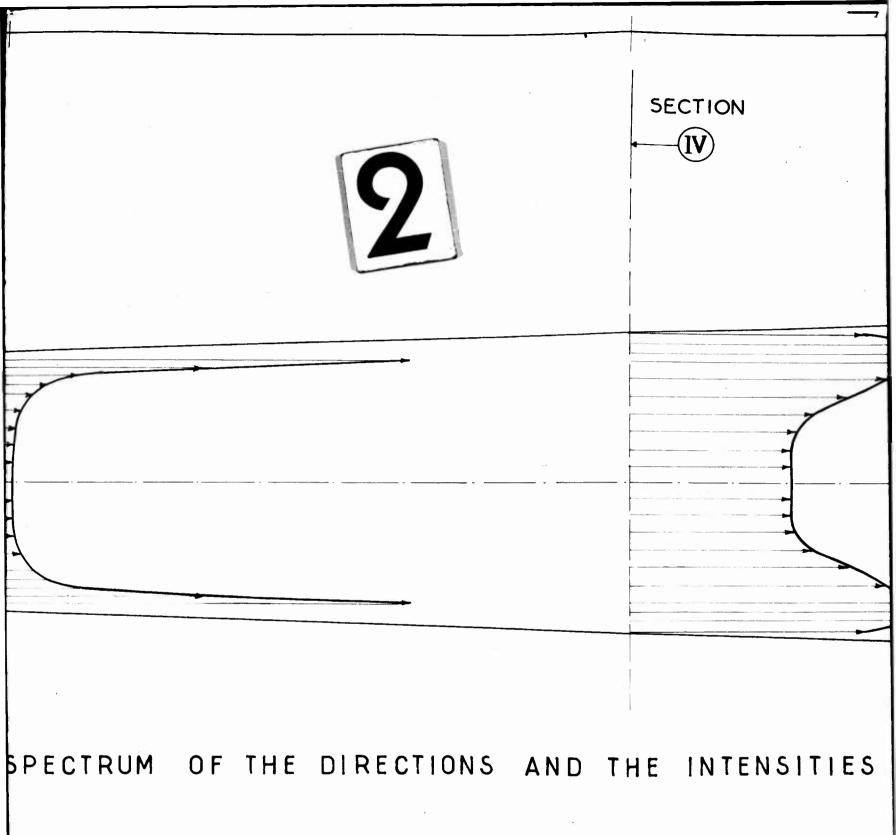
Effective static pressures plotted versus radii

Ps-Po g/cm² versus Rmm

at 
$$\frac{P_1.P_0}{P_0}$$
  $\begin{cases} 1.5 - 0.3 - 0.3 - 0.3 \end{cases}$ 



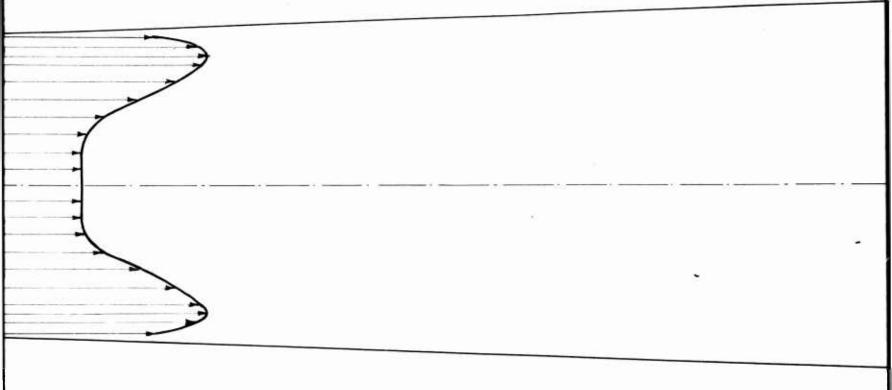




Scale: 1 cm = 20 m/

DИ





TENSITIES OF THE VELOCITIES IN DIFFERENT SECTIONS

1 cm = 20 
$$\frac{m}{s}$$
 at  $\frac{P_1 - P_0}{P_0} = 1.5$ 

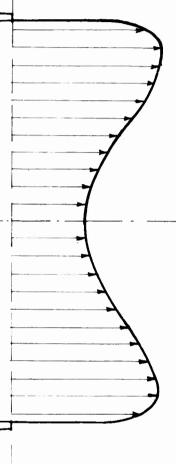
4

DIFFERENT SECTIONS OF THE NOZZLE

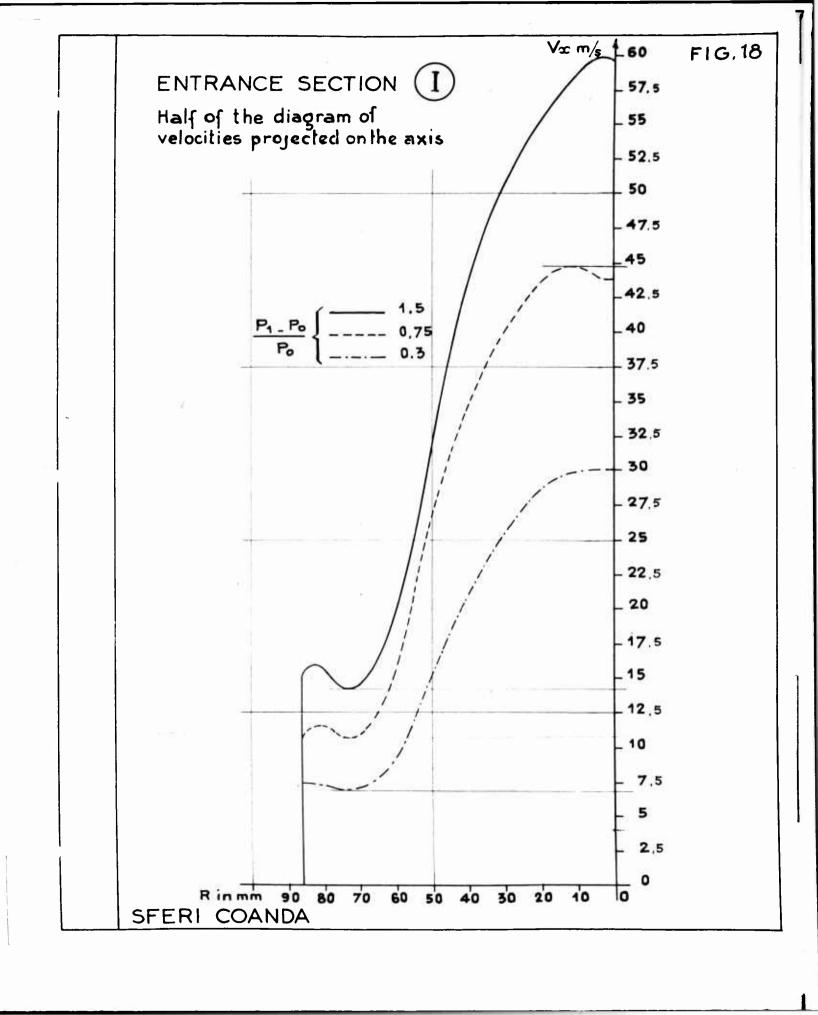
SECTION



5



F THE NOZZLE

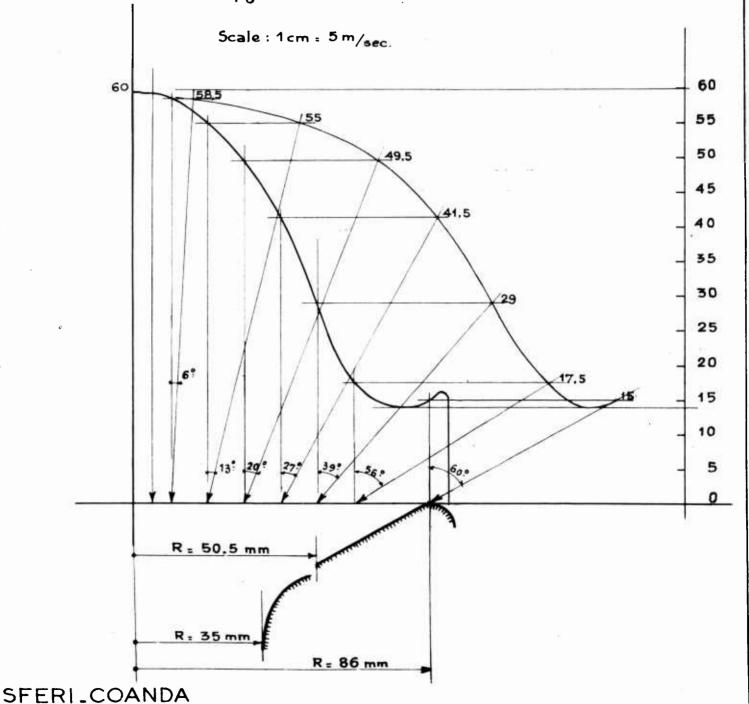


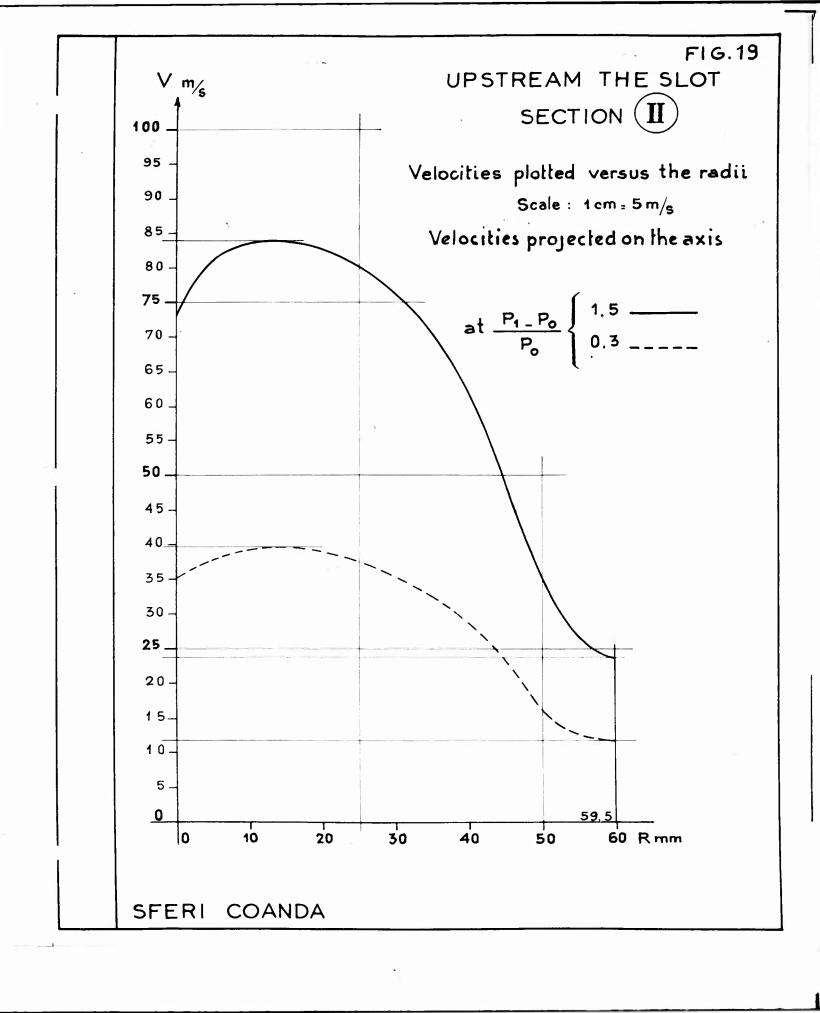
——— Half of the spectrum of velocities at the entrance (I) (in magnitude and direction.)

\_\_\_\_Half of the diagram of their projections on the direction of the axis.

$$\frac{P_1 - P_0}{P_0} = 1.5$$

Opening . 6 mm.



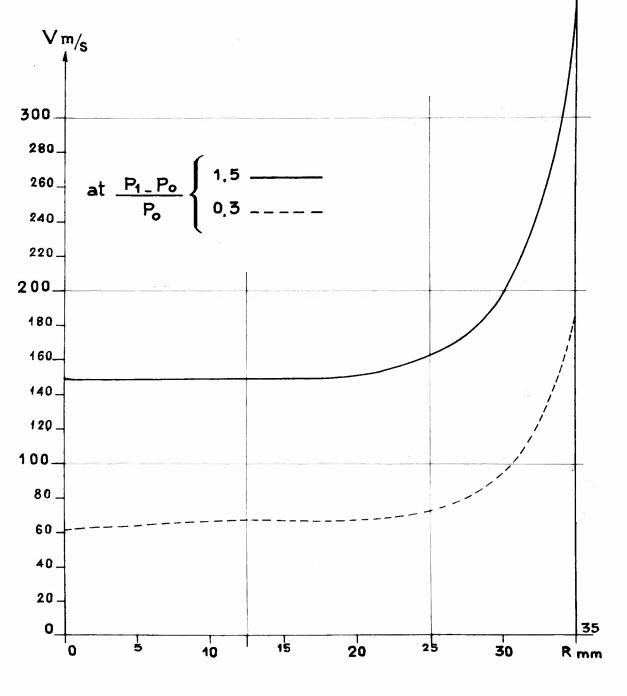


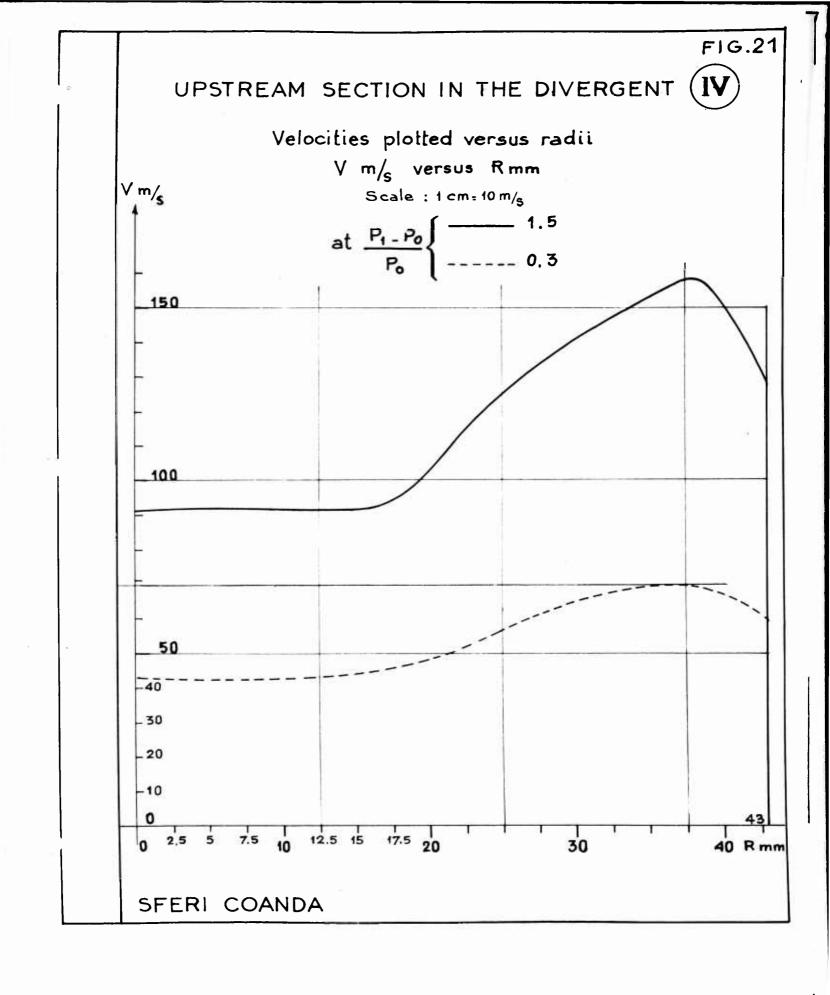
THROAT SECTION (III)

Velocities plotted versus radii

SFERI COANDA

Scale : 1 cm = 20 m/s



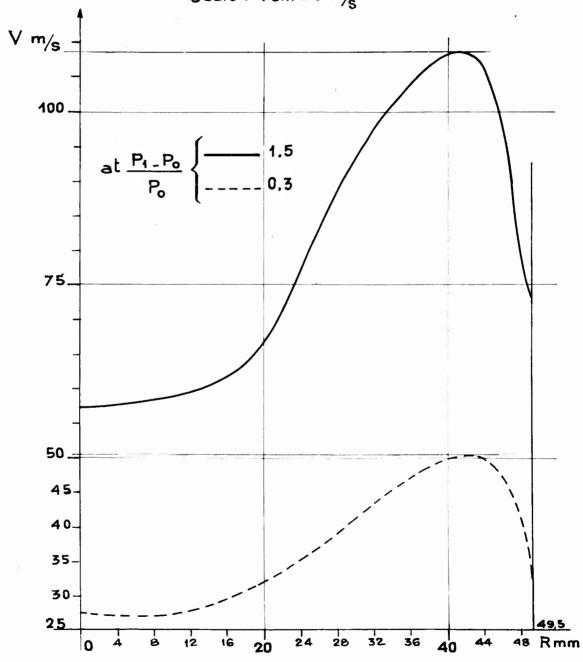


### DOWNSTREAM SECTION OF THE DIVERGENT (V)



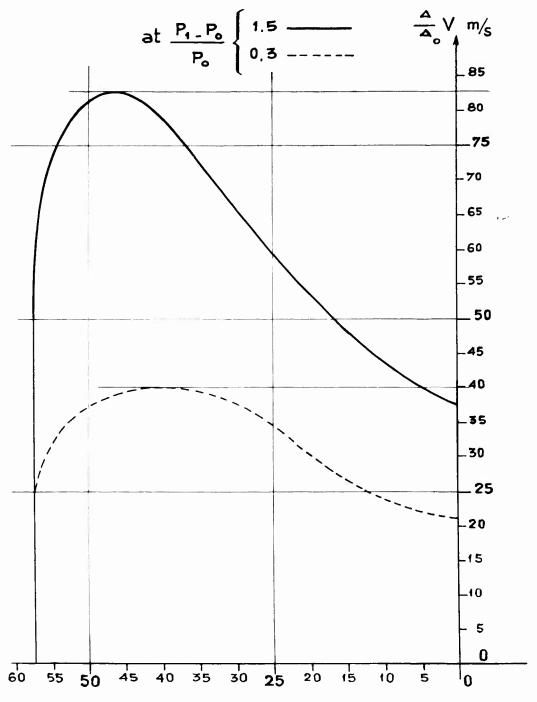
Velocities plotted versus radii Vm/s versus Rmm

Scale: 1 cm = 5 m/s

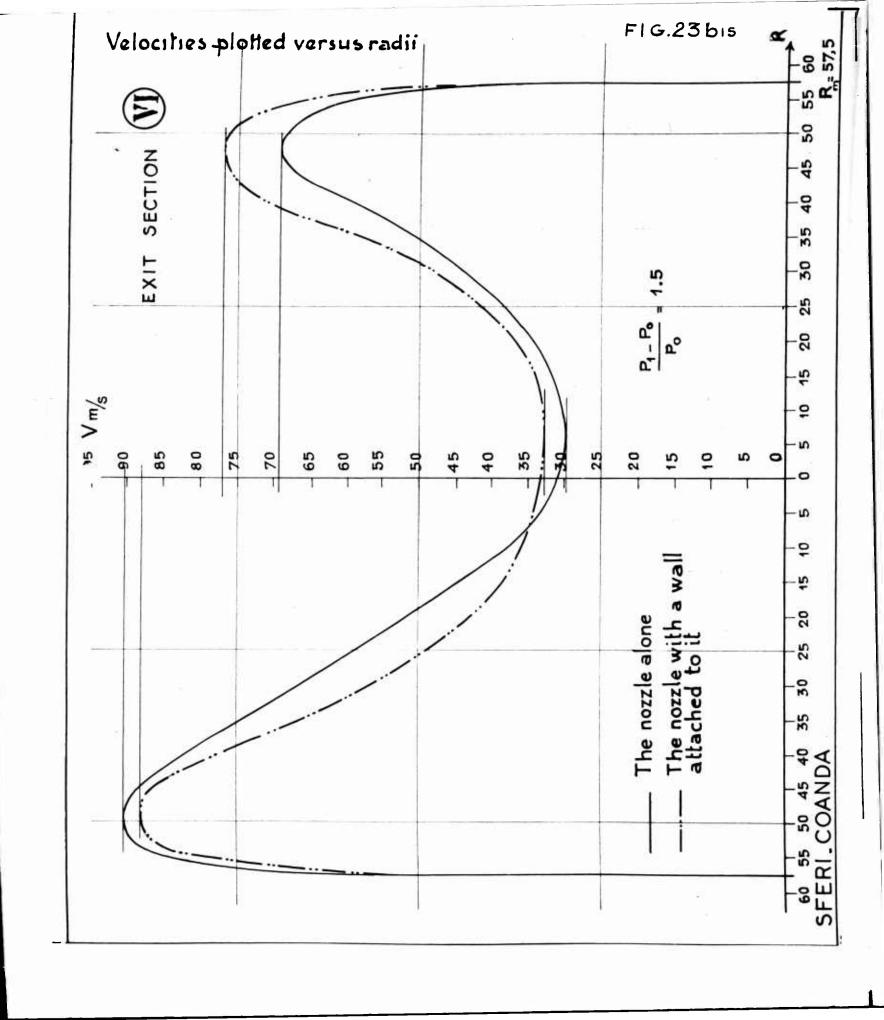


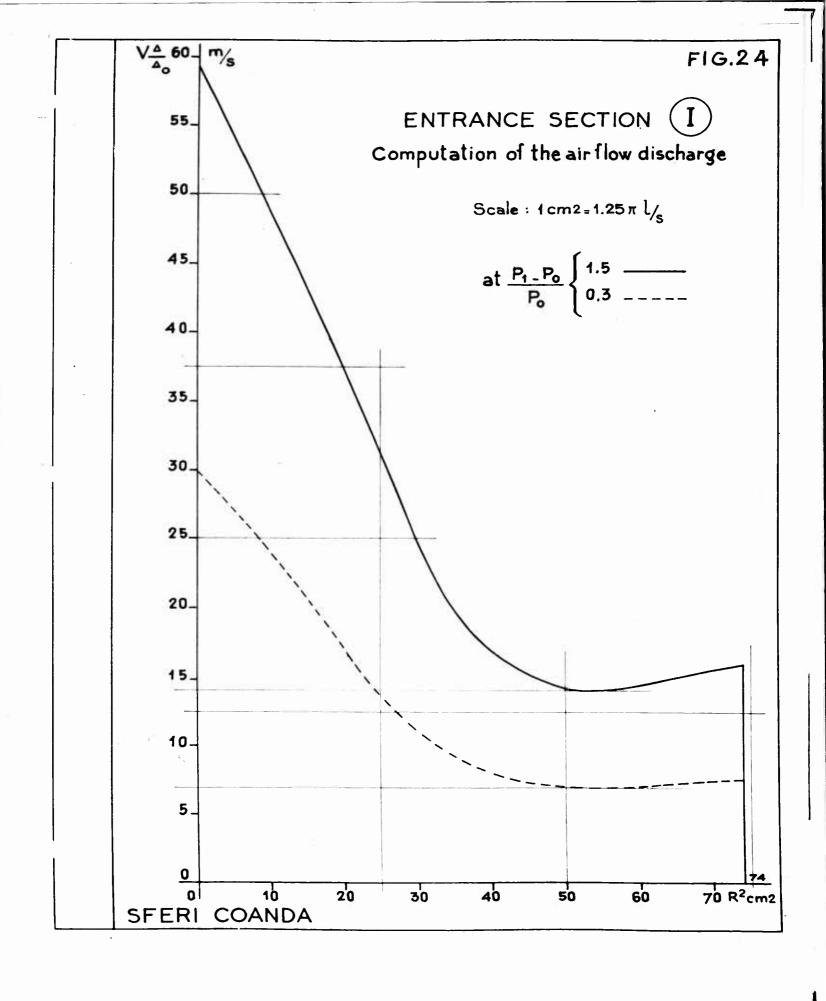


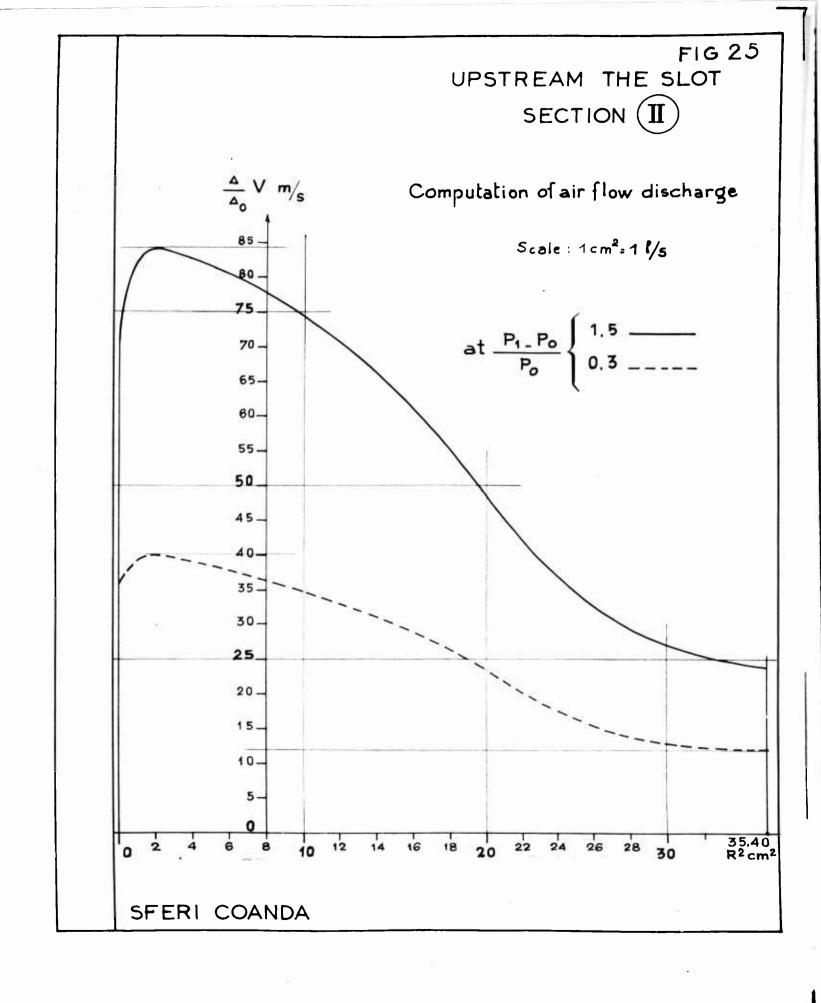
Velocities plotted versus radii Mean values



Scale: 1cm = 5 m/s



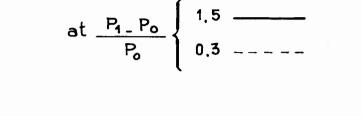


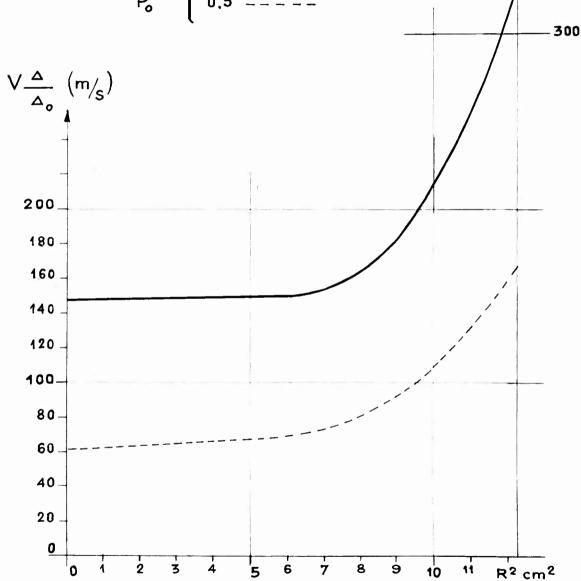


## THROAT SECTION (III)

Computation of the corrected air flow discharge

Scale: 1 cm2 = 2 1 l/s





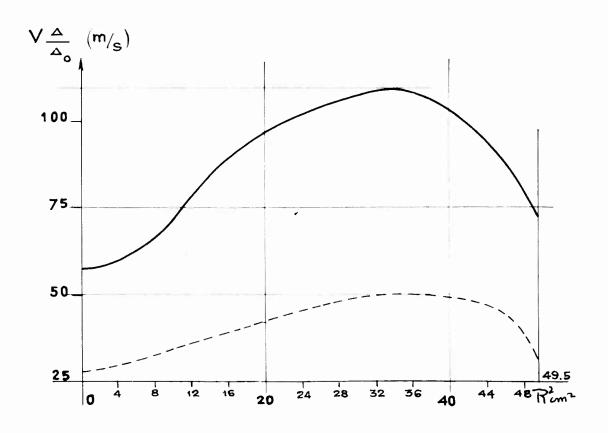
### DOWNSTREAM SECTION OF THE DIVERGENT

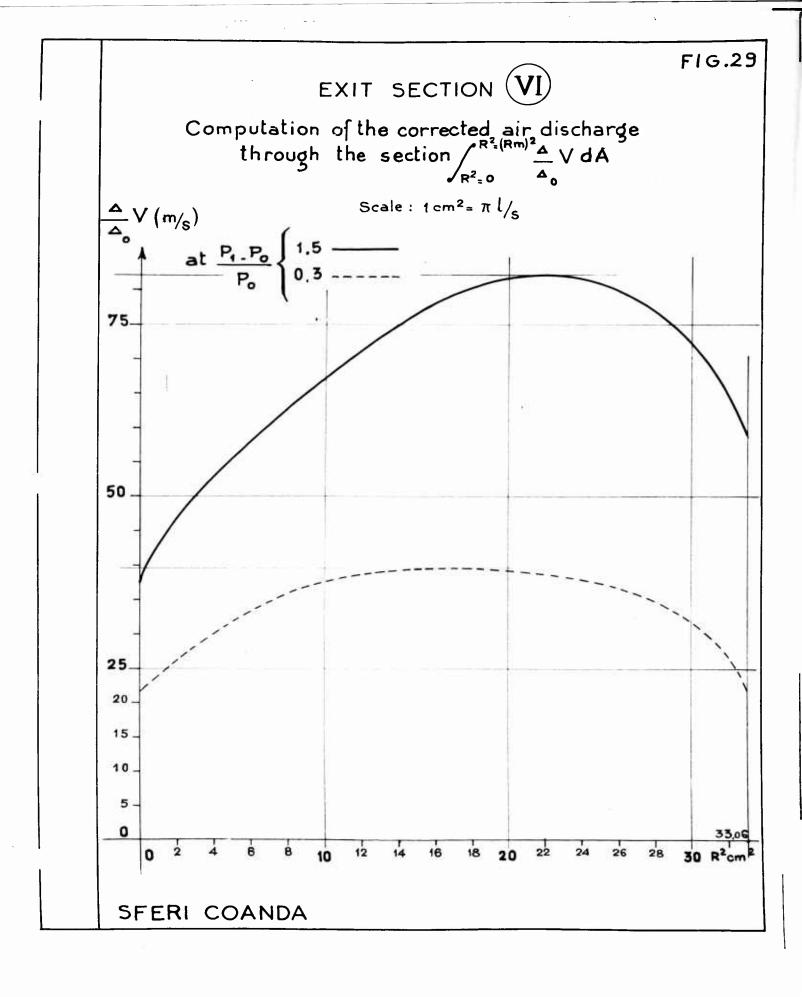


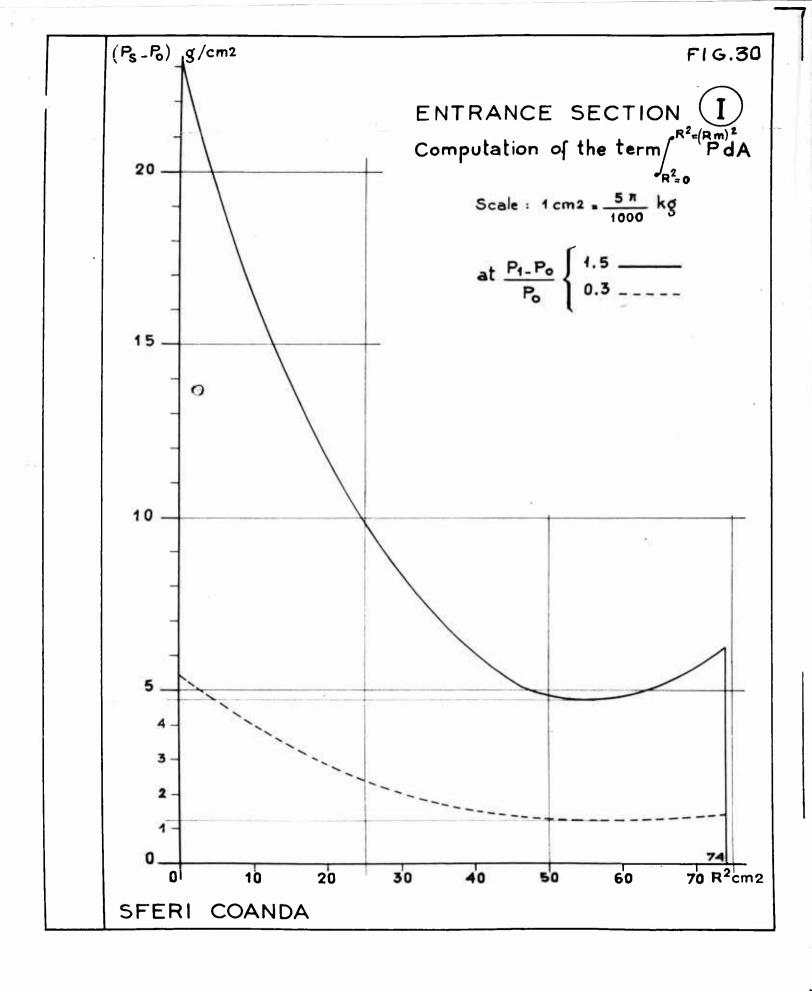
Computation of the corrected air discharge through the section  $\int_{R^2=0}^{R^2=(Rm)^2} \frac{\Delta}{\Delta_0} V dA$ 

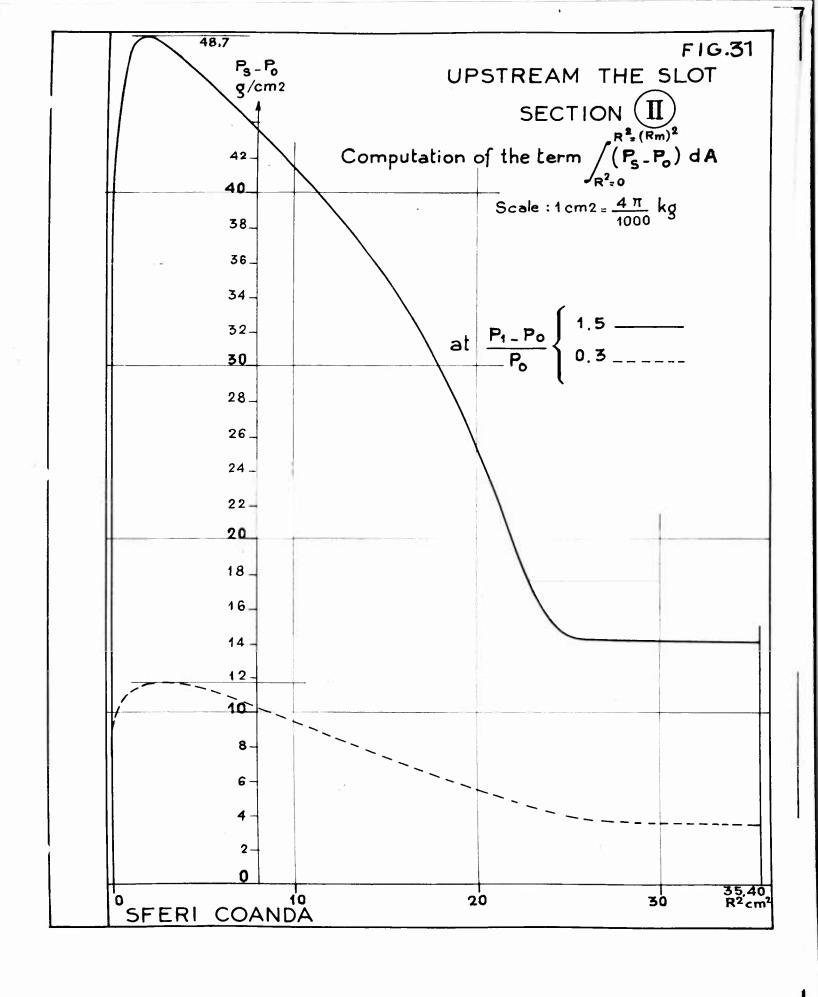
Scale: 1cm2 = Tl/s

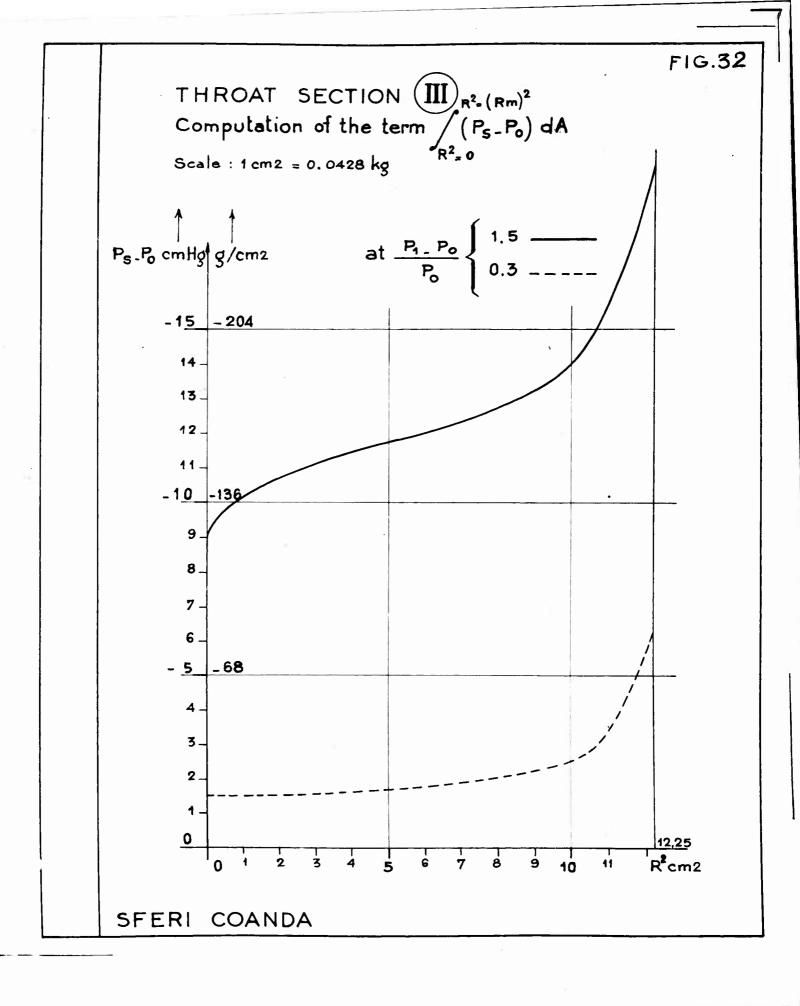
at 
$$\frac{P_1 P_0}{P_0}$$
  $\begin{cases} 1.5 - 0.3 - 0.3 \end{cases}$ 

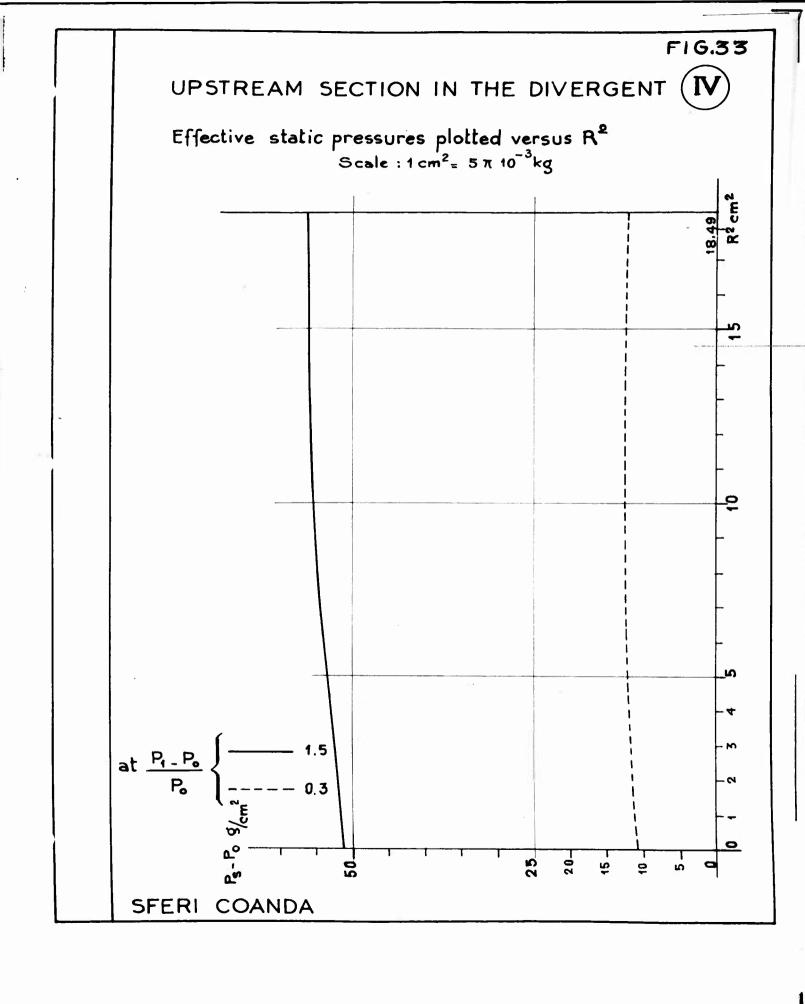








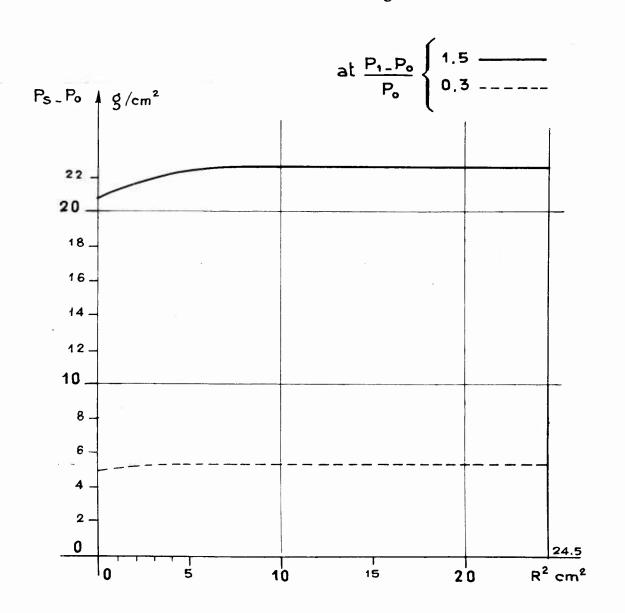




### DOWNSTREAM SECTION OF THE DIVERGENT



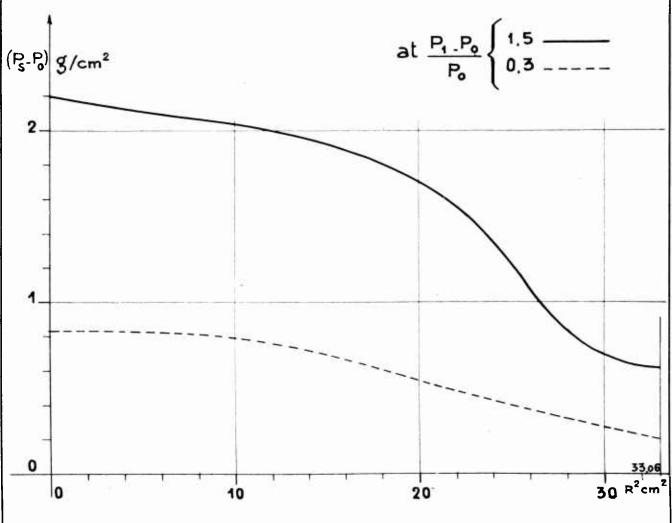
Scale: 1 cm2 = 4 \pi 10 3 kg



## EXIT SECTION (VI)

Computation of the pressure term  $\int_{R^2=0}^{R^2_+(R\ m)^2} (P_s - P_o) \ dA$   $P_s - P_o \ g/_{cm}^2 \text{ versus } R^2_{cm}^2$ 

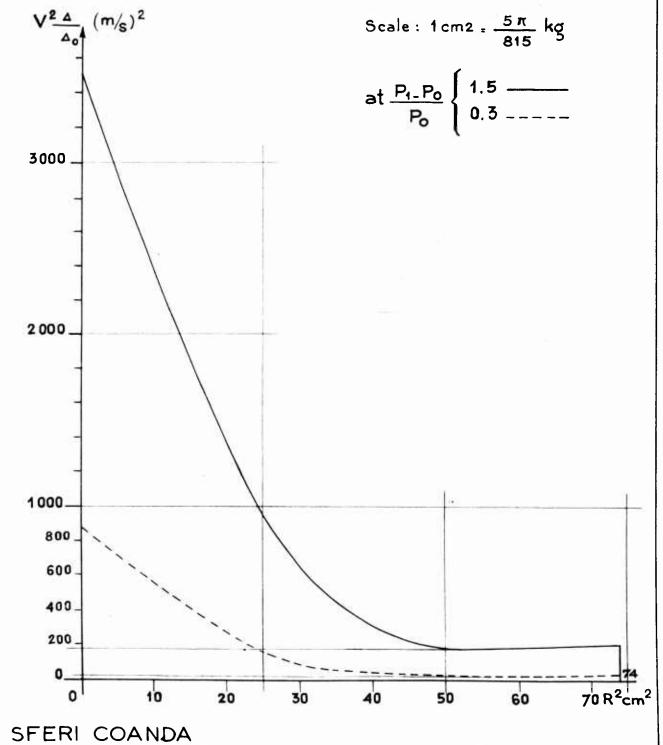
Scale: 1 cm2=4n10-4 kg

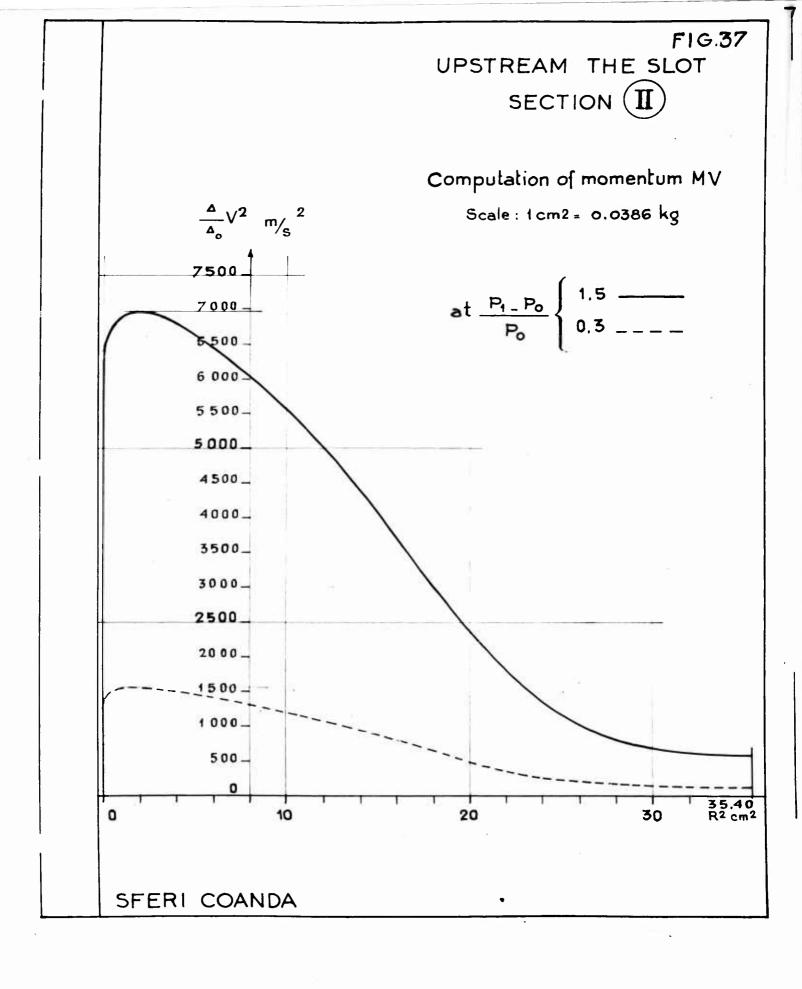


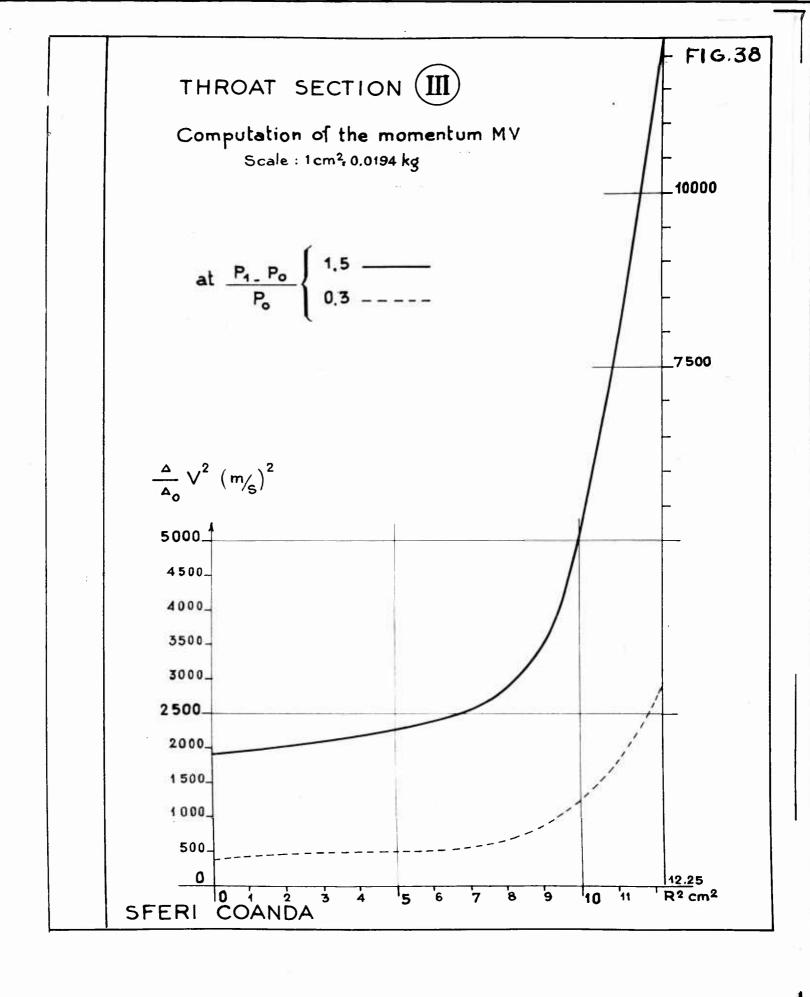
## ENTRANCE SECTION

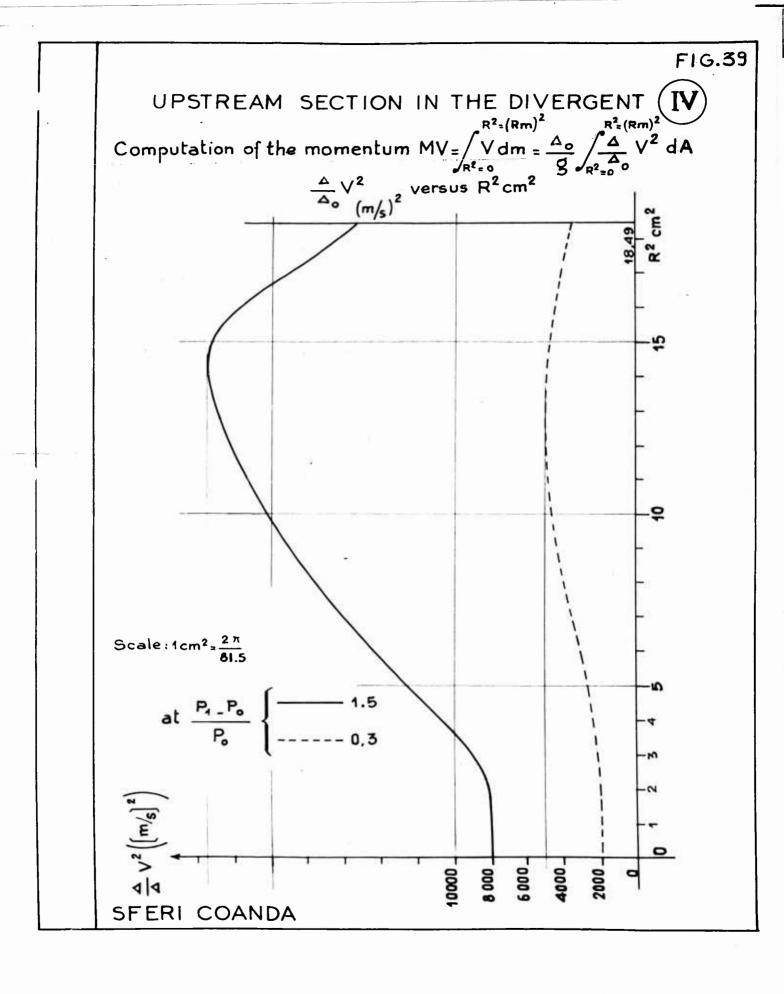


Computation of momentum MV







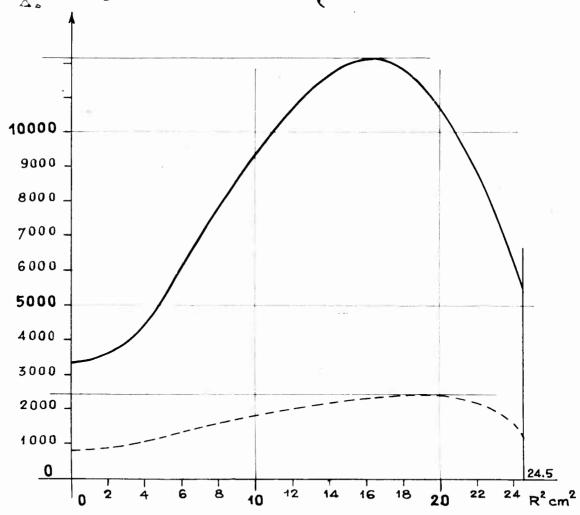


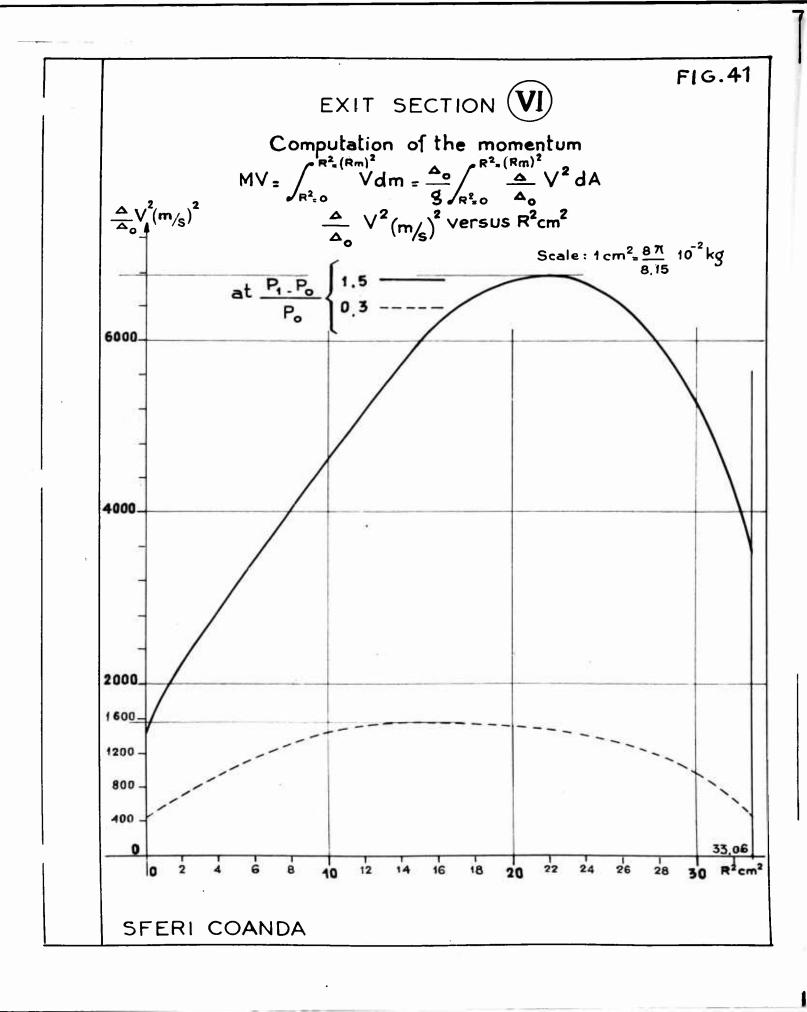
### DOWNSTREAM SECTION OF THE DIVERGENT



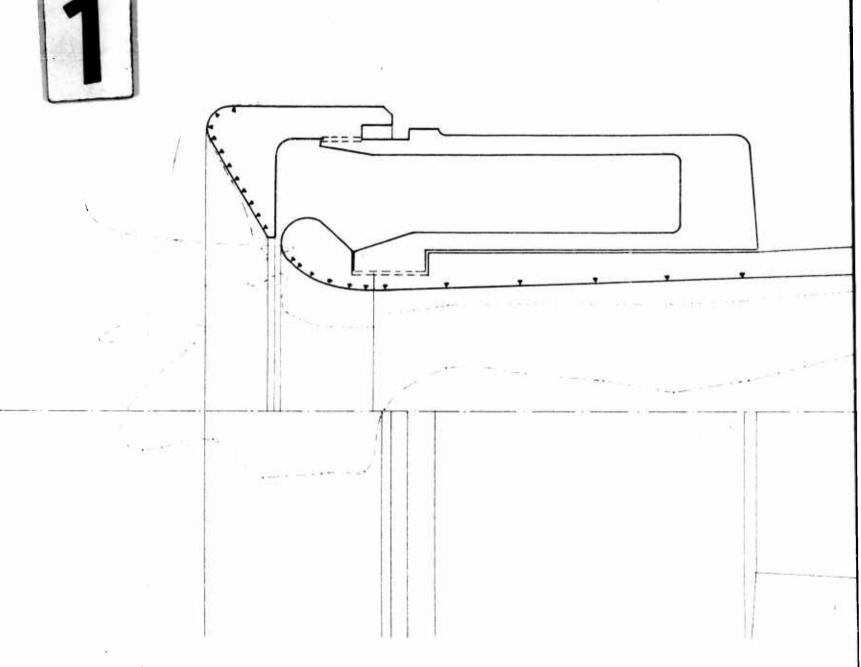
Computation of 
$$\frac{\Delta_o}{g} / \frac{\Delta_o}{R^2 + 0} \frac{\Delta}{\Delta_o} V^2 dA$$

$$\frac{\Delta}{\Delta_s} \bigvee^2 \left( \frac{m}{s} \right)^2 \qquad \text{at } \frac{P_1 P_0}{P_0} \begin{cases} 1.5 \\ 0.3 \\ --- \end{cases}$$





General view of the distribution of the depressions (Pw-Po) along the internal profile of the nozzle



General scale:  $1 \text{ cm} = 50 \text{ gr/cm}^2$  at this scale the pressures on the cap at  $\frac{P_1 - P_0}{P_0} = 0.3$  are not visible

SFERI-COANDA.

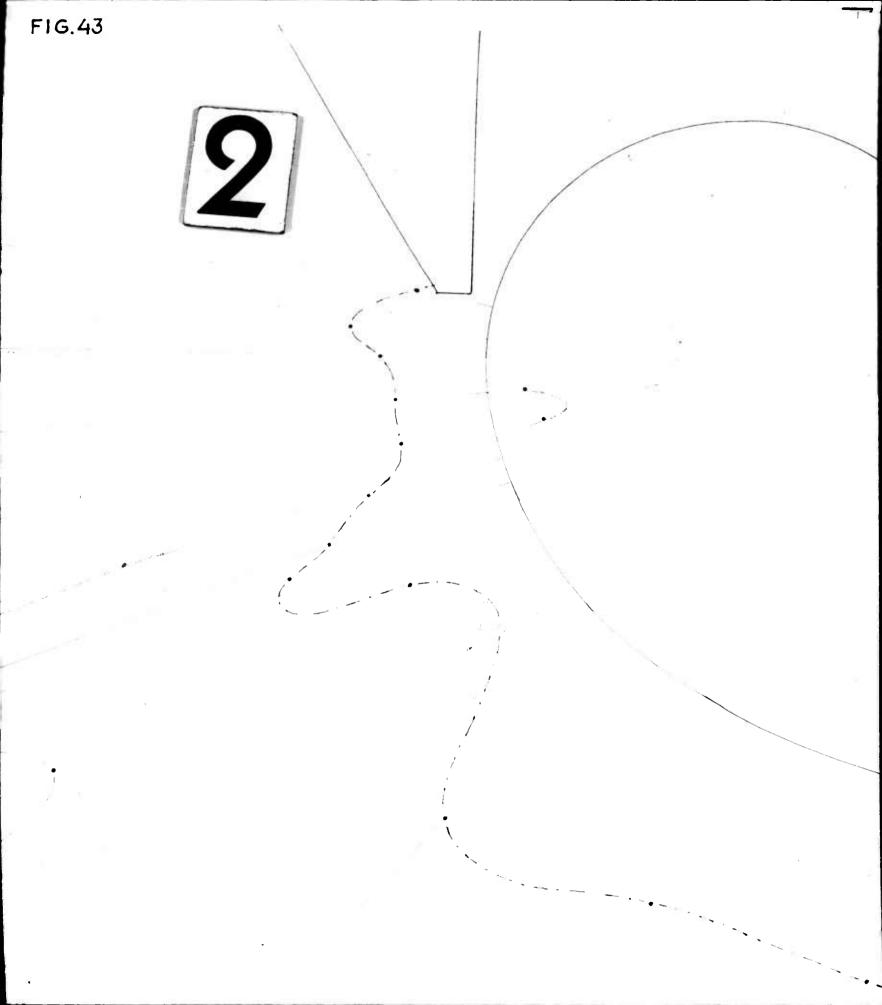
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- 1



Detailed view of the depressions (Rw\_Po) FIG.43 on the lip.





$$\frac{P_1 - P_0}{P_0}$$
 1.5  $\frac{\text{Kg}_{cm^2}}{0.3 \text{ Kg/cm}^2}$ 

Scale Icm = 10 gr/cm2

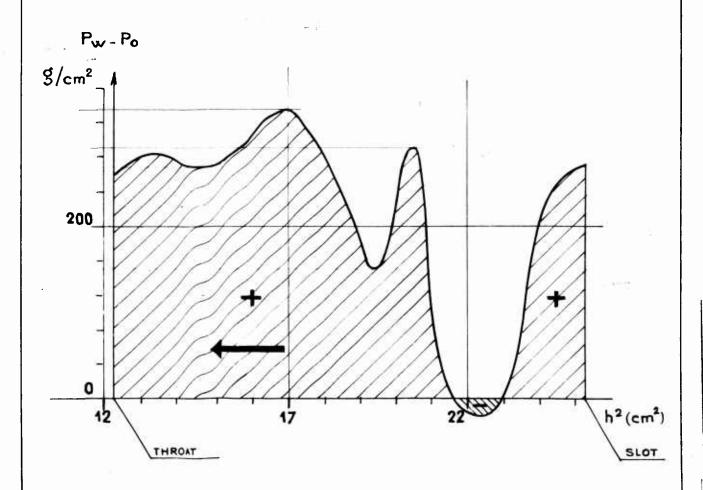


#### EFFECTIVE PRESSURES ON THE LIP

plotted versus the square of the distance to the axis.

 $P_{w} - P_{o} g/_{cm}^{2} \text{ versus } h^{2} \text{ cm}^{2}$ Scale:  $1 \text{ cm}^{2} = 4 \pi 10^{-2} \text{kg}$ 

at  $P_1 - P_0 = 1.5$ 



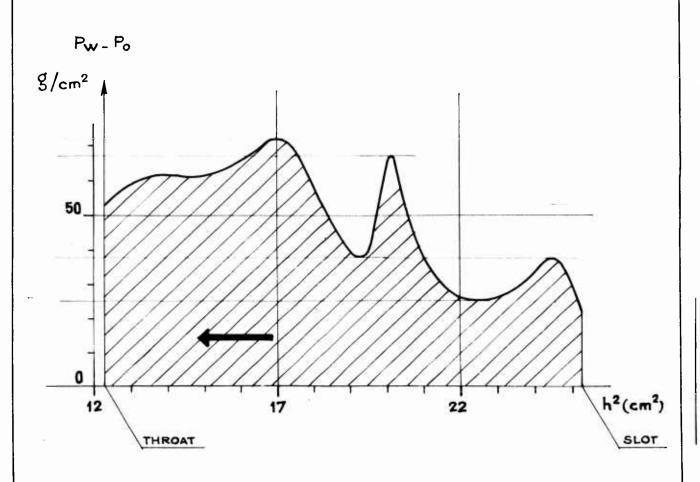
#### EFFECTIVE PRESSURES ON THE LIP

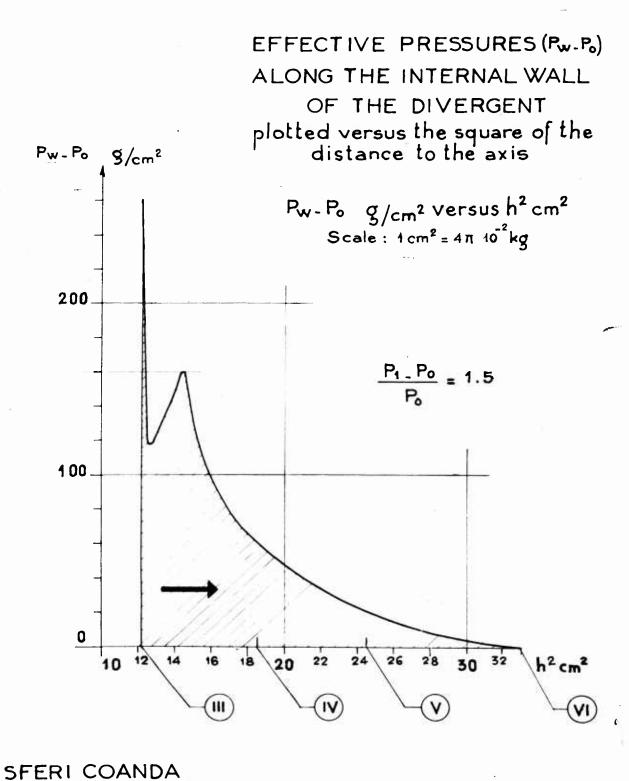
plotted versus the square of the distance to the axis.

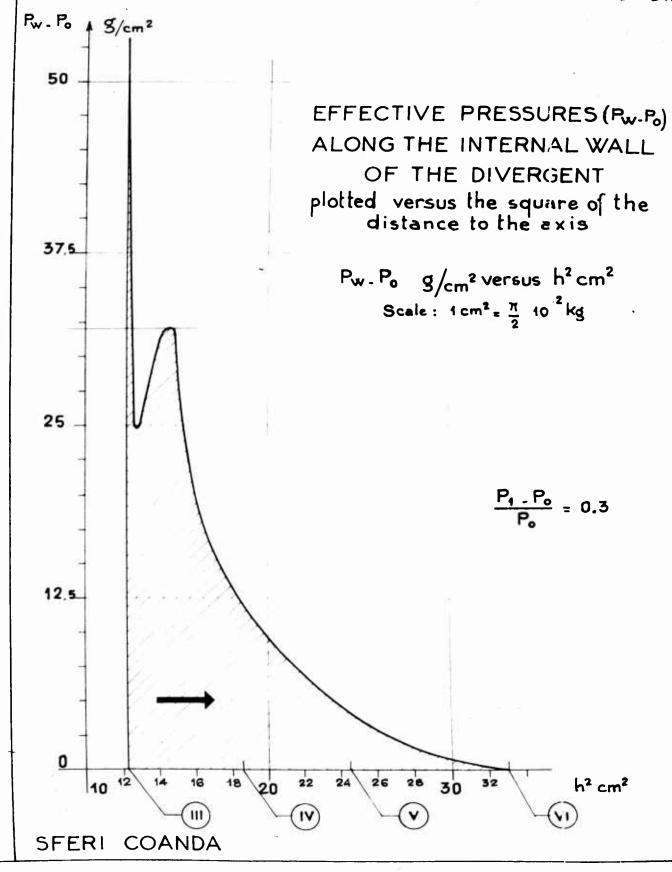
Pw-Po g/cm2 versus h2cm2

Scale: 
$$1 \text{cm}^2 = \frac{\pi}{100} \text{ kg}$$

at  $P_1 - P_0 = 0.3$ 







# UNCLASSIFIED

UNCLASSIFIED